

Take-home examination in Labor Economics, MA  
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Beginning: Tuesday, 21.2. 2006 at 12.00  
End: Monday, 27.2.2006 at 12.00

Consider the standard model of search. An infinitely lived workers meet employers according to a Poisson process with parameter  $\lambda s$ , where  $\lambda$  represents market conditions and  $s$  is the search effort of the worker. The cost of search is  $c(s)$ , where  $c(s)$  is convex and  $c(0) = 0$ . When the worker meets an employer, he receives a wage offer that is a random draw from a fixed distribution  $F(w)$ . There is an exogenous separation rate  $\delta$  and unemployed workers receive a fixed benefits flow,  $b$ .

**Part 1.** Suppose that search on the job is possible and the costs of search  $c(s)$  are the *same* if the worker is unemployed or works at *any* wage,  $w$ . Use the assumptions that, in a short interval  $h$ , the probability to meet employer is  $\lambda sh + O(h)$  and the probability to be thrown back into unemployment is  $\delta h + O(h)$  to formulate the Bellman equations and derive the asset equations that determine the value of being unemployed and the value of being employed at a wage  $w$ . (The function  $O(h)$  is a second order residual such that  $\frac{O(h)}{h}$  approaches 0 as  $h$  approaches 0.)

*Question 1.* Use the asset equations to determine the reservation policy and the search intensity in each possible state.

*Question 2* Describe the evolvement of search intensity, wages and quits as the worker ages.

*Question 3.* Define a stochastic stationary equilibrium and describe the impact of  $\lambda$ ,  $\delta$  and  $b$  on the steady state level of unemployment.

**Part 2.** Suppose that the worker searches *only* when unemployed at costs  $c(s)$ . Reformulate the Bellman equations and derive the asset equations that determine the value of being unemployed and the value of being employed at a wage  $w$ .

*Question 1.* Use the asset equations to determine the reservation wage  $R$  and the search intensity  $s$  when the worker is unemployed.

*Question 2* By eliminating the asset values  $W(w)$  and  $V$ , derive from the two asset equations and the first order condition for  $s$  two equations that jointly determine the optimal levels of  $s$  and  $R$ .

*Question 3.* Show that the reservation wage  $R$  must exceed  $b$ .

*Question 4.* Use the two simultaneous equations that determine  $s$  and  $R$  to show that both  $s$  and  $R$  rise if the distribution of wage offers  $F(w)$  is subject to a mean preserving increase in spread.

**Part 3.**

*Question 1.* What are the main testable implications of the search model?

*Question 2* Is it possible to separate search from investment as causes of individual wage growth?

Sources:

D. Mortensen (1986), "Job Search and Labor Market Analysis," O. Ashenfelter and R. Layard (eds.) *Handbook of Labor Economics* Volume 2.

D. Mortensen and C. Pissarides (1999), "New Developments in Models of Search in the Labor Markets," O. Ashenfelter D. Card (eds.) *Handbook of Labor Economics* Volume 2.

Y. Rubinstein and Y, Weiss (2005), "Post-Schooling Wage Growth: Investment, Search and Learning" Forthcoming in E. Hanushek and F. Welch (eds.) *Handbook of the Economics of Education*.