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Lecture 4: Machine Learning Techniques in Side-Channel Analysis

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Including presentation material by Guy Wolf

Outline



Introduction

- Side-Channel Leaks
- Machine Learning
- 2 Recap: Correlation Power Analysis
- 3 Template Power Analysis
 - Dimensionality Reduction
 - Classification
 - Power Trace Alignment

4 Activity Leaks

- Hidden Markov Model
- Acoustic Analysis of Peripherals
- Other Activity Leaks

5 Conclusion

Side-Channel Leaks



Side-Channel Leaks





Traces are vectors representing a measured physical quantity as a function of time, during the attacked operation. They containing hundreds or more (often millions) of measurement points.



leaked data







🗌 leaked data	



leaked data	



leaked data		
		$\subseteq \mathbb{R}^{1000000}$







Machine Learning

Machine learning encompasses tools that perform smart analysis of data, such as:

- Discovery of useful, possibly unexpected, patterns in data
- Non-trivial extraction of implicit, previously unknown and potentially useful information from data
- Exploration & analysis, by automatic or semi-automatic means, of large quantities of data in order to discover meaningful patterns

Common tasks include:

- Dimensionality reduction
- Clustering & Classification
- Regression & Out-of-sample extension



Typical assumption:

power consumption correlates with Hamming Weight of y



Traces matrix:

Hamming Weight matrix:



Traces matrix:

Hamming Weight matrix:



Traces matrix:

Hamming Weight matrix:



Correlation indicates the correct time and key



Hamming Weight matrix:



Correlation indicates the correct time and key

Alternative Attack: Template Power Analysis

Training: Learn traces of many plaintexts & keys times







Representing power traces as vectors

Traces are high-dimensional vectors, containing hundreds or more (often millions) of measurement points.



Traces can be analyzed as vectors in the Euclidean space \mathbb{R}^m with ℓ_2 norms & distances

• Somewhat arbitrary representation, but effective and convenient

Template Power Analysis Learning & analyzing trace vectors

Template assumption: the positions of traces in \mathbb{R}^m (with ℓ_2 norm) correlate with the plaintext & key values that generated them



Correlation is either directly seen or via some internal value
Ideally, correlation is expressed as clustering by plaintext & key
Theoretically, can detect clusters using *machine learning* tools too. Usually,
enough is known to classify traces into clusters; the challenge is to characterize
these clusters geometrically so we can check which cluster the online trace resides

Example: classic TPA attack using Gaussian statistical modeling¹

Model power consumption of encrypting plaintext p with key k as a random variable $\vec{X}_{(k,p)} \sim \mathcal{N}(\vec{\mu}_{(k,p)}, \Sigma_{(k,p)})$

- $\vec{X}_{(k,p)}$ is drawn from a multidimensional normal (Gaussian) distribution
- $\vec{\mu}_{(k,p)} \in \mathbb{R}^m$ is the mean power consumption for $k \And p$
- $\Sigma_{(k,p)}$ is the $m \times m$ noise covariance matrix for $k \And p$
- The likelihood of a trace \vec{x} originating from k & p is $\mathcal{L}_{(k,p)}(\vec{x}) = \left((2\pi)^m |\Sigma_{(k,p)}|\right)^{-1/2} \exp\left(-\frac{1}{2}(\vec{x} - \vec{\mu}_{(k,p)})^T \Sigma_{(k,p)}^{-1}(\vec{x} - \vec{\mu}_{(k,p)})\right)$

Attack single trace (with known plaintext p):

- Compute likelihood of it originating from each key candidate (with p)
- Choose key candidate with maximum likelihood

¹ "Template Attacks", 2003, by S. Chari, J.R. Rao, and P. Rohatgi

Curse of dimensionality

Directly analyzing high-dimensional vectors is usually infeasible due to:

Curse of Dimensionality

A general term for various phenomena that arise when analyzing/organizing high-dimensional data.

- Common theme difficult/impractical/impossible to obtain statistical significance due to sparsity of the data in high-dimensions
- Causes poor performance (computational complexity)
- Causes poor results (bad estimates)

Common solution - use **dimensionality reduction** methods and analyze their resulting embedded space.

Example: only use the $\ell < m$ time indices that provide the highest differences between mean power consumptions of different key-plaintext pairs. This is traditional *differential power analysis*.

Dimensionality Reduction with Principal Component Analysis

Dimensionality Reduction Principal Component Analysis (PCA)

3D space

Dimensionality Reduction Principal Component Analysis (PCA)



Dimensionality Reduction Principal Component Analysis (PCA)



Dimensionality Reduction

Principal Component Analysis (PCA) - covariance matrix



$$cov(t_1, t_2) \triangleq \sum_i trace_i[t_1] \cdot trace_i[t_2]$$

Dimensionality Reduction

Principal Component Analysis (PCA) - spectral theorem



Spectral Theorem: $COV(t_1, t_2) = \sum_i \lambda_i \phi_i(t_1) \phi_i(t_2)$

Dimensionality Reduction

Principal Component Analysis (PCA) - truncated SVD



Many datasets (incl. power traces) have a decaying cov. spectrum
Principal Component Analysis (PCA) - truncated SVD



Approximate cov. matrix by truncating small eigenvalues from SVD

Principal Component Analysis (PCA) - example

Consider simple case of traces that are all on the same high dimensional line

- Straight line is defined by a unit vector $\left\|ec{\psi}
 ight\|=1$
- \bullet Points on the line are defined by multiplying $\vec{\psi}$ by scalars
- The traces can be formulated as $x_i = c_i \vec{\psi}$
- Covariance: $\operatorname{cov}(t_1, t_2) = \sum_i x_i[t_1] x_i[t_2] = \sum_i c_i \vec{\psi}[t_1] c_i \vec{\psi}[t_2] = (\sum_i c_i^2) \vec{\psi}[t_1] \vec{\psi}[t_2] = \|\vec{c}\|^2 \vec{\psi}(t_1) \vec{\psi}(t_2) \qquad \vec{c} \triangleq (c_1, c_2, \ldots)$



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Covariance matrix has a single eigenvalue $\|\vec{c}\|^2$ and a single eigenvector $\vec{\psi}$, which defines principal direction of the trace-vectors







Principal Component Analysis (PCA) - example



principal components \Rightarrow max var directions

Principal Component Analysis (PCA) - projection

Projection on principal components:



Dimensionality Reduction Principal Component Analysis (PCA) - projection

Projection on principal components:



PCA algorithm

PCA algorithm:

Centering

- Ovariance
- eigendecomposition
- Projection

Alternative method: Multi-Dimensional Scaling (MDS) - preserve distances/inner-products with minimal set of coordinates.

Short tutorial on PCA & MDS: www.cs.haifa.ac.il/~rita/uml_course/lectures/PCA_MDS.pdf

Dimensionality Reduction Summary



Dimensionality Reduction Summary



Next task: how to find keys from the low-dimensional vectors?

Clustering & Classification with Support Vector Machine

Clustering

Cluster analysis

Clustering - the task of grouping objects such that objects in the **same cluster** are more **similar** to each other than to those in other clusters.



Clustering

Cluster analysis

Clustering - the task of grouping objects such that objects in the **same cluster** are more **similar** to each other than to those in other clusters.



Learning types

Unsupervised learning: Trying to find hidden structures in unlabeled data. Supervised learning: Inferring functions from labeled training data.

Clustering & classification approaches

Classic TPA using Gaussian statistical models:

- The analysis considers many clusters (one for each key-plaintext pair)
- Clusters are assumed to look like normally distributed random variables $\vec{X}_{(k,p)} \sim \mathcal{N}(\vec{\mu}_{(k,p)}, \Sigma_{(k,p)})$
- Requires many traces for each key-plaintext pair to compute $\vec{\mu}_{(k,p)}$ & $\Sigma_{(k,p)}$

Simplified bit clustering with Support Vector Machine (SVM):

- Classify each bit separately only two classes are considered for each bit
- Requires less training traces than classic TPA traces are grouped by bit values, not by the key value
- No statistical assumptions required geometric classification using a separating hyperplane

Simplified bit clustering - only two classes















Support Vector Machine (SVM) - quantifying robustness with margins



Support Vector Machine (SVM) - quantifying robustness with margins



SVM formulation - hyperplane



SVM formulation - hyperplane with margin



SVM formulation - shifted hyperplane with margin



SVM algorithm

SVM training

Input:

- Points $\{\vec{x}_i\}$ from PCA of the traces
- Labels $\{b_i\}$ according to attacked bit:

$$b_i = egin{cases} 1 & ext{bit is 0} \ -1 & ext{bit is 1} \end{cases}$$

Solve the quadratic program (e.g., using Lagrange multipliers):

Find $\max \alpha$ s.t. $\vec{w} \cdot \vec{x_i} - c \ge b_i \alpha$

Output: the solution (\vec{w}, c, α)

SVM algorithm

SVM classifier

Input:

- New point \vec{x} from PCA projection of attacked trace
- The solution (\vec{w}, c, α) from SVM training

Classify by value of $\vec{w} \cdot \vec{x} - c$:



Power Analysis with PCA & SVM based on recent paper²



Use single PCA & multiple SVMs (one per bit)

to learn traces (in training phase) and attack a key byte

²"Side channel attack: an approach based on machine learning", 2011, by L. Lerman, G. Bontempi, and O. Markowitch

Power Analysis with PCA & SVM based on recent paper²

PCA results (colored by specified bit values):



Empirical results (on 3DES): desc. success rate (by bit position) 7th bit success rate: \sim 95% \longrightarrow 1st bit success rate: \sim 50% ²"Side channel attack: an approach based on machine learning", 2011, by L. Lerman, G. Bontempi, and O. Markowitch

Power Trace Alignment

Power Trace Alignment

Motivation

Power traces can be misaligned for several reasons, such as

- Synchronization issues between the sampling devices and the tested hardware
- Clock variabilities and instabilities
- Intentional countermeasures such as delays and modulations

Misaligned traces \Rightarrow incorrect/inaccurate correlations \Rightarrow wrong classification and useless attacks

Power Trace Alignment

Naïve approach: static alignment by time offset


Naïve approach: static alignment by time offset



Naïve approach: static alignment by time offset



Naïve approach: static alignment by time offset



Machine-learning approach: adaptive alignment by Dynamic Time Warp (DTW)



Machine-learning approach: adaptive alignment by Dynamic Time Warp (DTW)



Machine-learning approach: adaptive alignment by Dynamic Time Warp (DTW)



Using pairwise alignment in an attack

Training:

- Acquire power traces
- One of all trace (e.g., arbitrarily or use mean of all traces)
- Align each trace to the reference trace using the pairwise alignment
- Apply training algorithm (e.g., PCA & SVM) to the aligned traces

Online:

- Acquire trace from attacked hardware
- Align trace to the reference trace (from the training) using pairwise alignment
- SApply classification algorithm (e.g., PCA & SVM)











Extreme offset: complete misalignment worst alignment alternative

Aligned distance:

$$\sum \left(\left| \right|^2 \right)^2 = \|x\|^2 + \|y\|^2$$



Finding optimal pairwise alignment





Dynamic Programming

- A method for solving complex problems by breaking them down into simpler subproblems.
- Applicable to problems exhibiting the properties of overlapping subproblems and optimal substructure.
- Better performances than naive methods that do not utilize the subproblem overlap.

Power Trace Alignment Dynamic Time Warp (DTW)

Basic DTW Algorithm:

For each trace-time *i* and for each trace-time *j*:

• Set
$$cost \leftarrow (x[i] - y[j])^2$$

• Set the optimal distance at stage [i, j] to:

Optimal distance: $DTW_{[m,n]}$ (where m & n are lengths of traces).

Optimal alignment: backtracking the path leading to $DTW_{[m,n]}$ via min-cost choices of the algorithm

Use coarse-grained matrices to avoid bad/unreasonable portions:



Drill down by fine graining to approximate the optimal alignment with quasi-linear time & space requirements

 $^{3} ^{\prime\prime} Improving Differential Power Analysis by Elastic Alignment'', 2011, by J.G.J. van Woudenberg, M.F. Witteman, and B. Bakker$

Experimental results:

Compare correlation DPA using 3 alignment methods:

Static: Simple static alignment by time offset

- SW: Replace trace entries with avg. of sliding window
 - Not strictly an alignment method, but simple & sometimes effective

DTW: Elastic alignment with DTW

³"Improving Differential Power Analysis by Elastic Alignment", 2011, by J.G.J. van Woudenberg, M.F. Witteman, and B. Bakker



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Analyzing Non-Cryptographic Leaks with Hidden Markov Model

Information & Activity Leaks

Consider secret sequence of activities and leaked information with the following properties:

- Contains information about the secret sequence
- Contains noise
- Insufficient for directly recovering the secret information

If activities follow **known statistical patterns**, then an attacker can **"guess" secret sequence** from noisy leaks.

Attack: find best hypothesis such that:

- It matches the leaked data
- Has high probability according to statistical distribution of activity sequences

Information & Activity Leaks

Can it work?

Leaked information can be used for more than cryptographic purposes:

- Users are predictable most activities are similar & repetitive
 - Internet common websites and surfing routines
 - Emails/documents linguistic models
 - Passwords most common password is "password"
 - Others examples: "querty", "letmein", "trustno1", "dragon", "monkey", "ninja", and "jesus".
 - $\bullet\,$ News services often publish lists of most common passwords of the year/month
- Guess activities/information by detecting "reasonable" usage patterns from leaked data

A statistical model of user activity profile can be used for this task.



Transition probabilities:

$$\Pr[q_{i+1} = ? | q_i, q_{i-1}, \dots, q_2, q_1]$$



Transition probabilities (no history):

$$\Pr[q_{i+1} = ? | q_i] = \Pr[q_{i+1} = ? | q_i, q_{i-1}, \dots, q_2, q_1]$$



















Viterbi Algorithm

A dynamic programming algorithm for finding the most likely sequence of hidden states, especially in the context of Hidden Markov models.

Acoustic Analysis of Keyboards $based on paper^4$



 $^{4}\mbox{``Keyboard}$ Acoustic Emanations Revisited",2005, by L. Zhuang, F. Zhou, and J.D. Tygar

Acoustic Analysis of Keyboards based on paper⁴



(b) Recognition Phase: Recognize keystrokes using the classifier from (a).

 $^{\rm 4}{\rm ``Keyboard}$ Acoustic Emanations Revisited'',2005, by L. Zhuang, F. Zhou, and J.D. Tygar

Acoustic Analysis of Keyboards based on paper⁴

Typed text:

the big money fight has drawn the support of dozens of companies in the entertainment industry as well as attorneys <u>gnnerals</u> in states, who fear the file sharing software will encourage illegal activity, stem the growth of small artists and lead to lost jobs and <u>dimished</u> sales tax revenue.

 $^{^{\}rm 4}{\rm ``Keyboard}$ Acoustic Emanations Revisited'',2005, by L. Zhuang, F. Zhou, and J.D. Tygar

Acoustic Analysis of Keyboards $_{\rm based \ on \ paper^4}$

HMM only:

the big money fight has drawn the <u>shoporo</u> <u>od dosens</u> of companies in the entertainment industry as well as attorneys <u>gnnerals on</u> states, who fear the <u>fild shading softwate</u> will encourage illegal <u>acyivitt</u>, <u>srem</u> the <u>grosth</u> of small <u>arrists</u> and lead to lost <u>cobs</u> and dimished sales <u>tas</u> revenue.

 $^{^{\}rm 4}{\rm ``Keyboard}$ Acoustic Emanations Revisited'',2005, by L. Zhuang, F. Zhou, and J.D. Tygar
Acoustic Analysis of Keyboards $based on paper^4$

HMM & spelling corrections:

the big money fight has drawn the support of dozens of companies in the entertainment industry as well as attorneys generals in states, who fear the <u>film</u> sharing software will encourage illegal activity, stem the growth of small artists and lead to lost jobs and <u>finished</u> sales tax revenue.

 $^{^{\}rm 4}{\rm ``Keyboard}$ Acoustic Emanations Revisited'',2005, by L. Zhuang, F. Zhou, and J.D. Tygar

Acoustic Analysis of Keyboards $based on paper^4$



 $^{4}\mbox{``Keyboard}$ Acoustic Emanations Revisited'',2005, by L. Zhuang, F. Zhou, and J.D. Tygar

Acoustic Analysis of Printers $based on paper^5$



(Picture taken from URL:flylib.com/books/en/2.374.1.27/1/)

URL:mindmachine.co.uk/book/print_06_dotmatrix_overview01.html)

⁵ "Acoustic Side-Channel Attacks on Printers",2010, by M. Backes, M. Dürmuth, S. Gerling, M. Pinkal, C. Sporleder

Acoustic Analysis of Printers based on paper⁵



⁵"Acoustic Side-Channel Attacks on Printers",2010, by M. Backes, M. Dürmuth, S. Gerling, M. Pinkal, C. Sporleder

Acoustic Analysis of Printers based on paper⁵

Training:

- Feature extraction (split into words, noise reduction, etc.)
- Construct DB with (word, sound) pairs

Online:

- Feature extraction (same as in training)
- For each word:
 - Sort DB by similarity/difference from recorded sound
 - Reorder DB by n-gram/word distribution using HMM
 - Guess printed word as the top candidate from reordered DB

⁵"Acoustic Side-Channel Attacks on Printers",2010, by M. Backes, M. Dürmuth, S. Gerling, M. Pinkal, C. Sporleder

Acoustic Analysis of Printers based on paper⁵

	Text 1	Text 2	Text 3	Text 4		Overall	
asic Top 1 (<i>Top 3</i>) MM 3-gram	60.5 % (75.1 %) 66.7 %	66.5 % (79.2 %) 71.8 %	62.8 % (78.7 %) 71.2 %	61.5 % (77. 9 %) 69.0 %		62.9 % (78.0 %) 69.9 %	
			Declaratio	n 1	Decla	ration 2	
Basic Top 1 (<i>Top 3</i>) HMM 3-gram (using general-purpose corpus) HMM 3-gram (using domain-specific corpus)			59.5 % (7	7.8 %)	57.5 9	$\%(72.6\ \%)$	

⁵ "Acoustic Side-Channel Attacks on Printers",2010, by M. Backes, M. Dürmuth, S. Gerling, M. Pinkal, C. Sporleder

Other Activity Leaks

Other activity leaks to which machine learning (and other tools) are applied:

- Offensively:
 - Other cases of trace analysis (e.g., frequency domain)
 - Traffic analysis
 - Deanonymization
- Defensively:
 - Authentication
 - Malware code detection
 - Malware command-and-control traffic detection
 - DDoS detection

Further Reading I

Side-channel attacks using machine learning tools:

- "Further hidden Markov model cryptanalysis" (2005) by P.J. Green, R. Noad, N.P. Smart
- "Analyzing side channel leakage of masked implementations with stochastic methods" (2007) by K. Lemke-Rust & C. Paar
- "Side channel attacks on cryptographic devices as a classification problem" (2007) by P. Karsmakers, B. Gierlichs, K. Pelckmans, K. De Cock, J. Suykens, B. Preneel, B. De Moor
- "Theoretical and practical aspects of mutual information based side channel analysis" (2009) by E. Prouff & M. Rivain
- "Cache-timing template attacks" (2009) by B.B. Brumley & R.M. Hakala

- "Machine learning in side-channel analysis: a first study" (2011) by G. Hospodar, B. Gierlichs, E. De Mulder, I. Verbauwhede, J. Vandewalle
- "Side channel attack: an approach based on machine learning" (2011) by L. Lerman, G. Bontempi, O. Markowitch
- "Side channel cryptanalysis using machine learning" (2012) by H. He, J. Jaffe, & L. Zou
- "PCA, eigenvector localization and clustering for side-channel attacks on cryptographic hardware devices" (2012) by D. Mavroeidis, L. Batina, T. van Laarhoven, E. Marchiori
- "Efficient Template Attacks Based on Probabilistic Multi-class Support Vector Machines" (2013) by T. Bartkewitz & K. Lemke-Rust

Further Reading II

Trace alignment:

- "Recovering secret keys from weak side channel traces of differing lengths" (2008) by C.D. Walter
- "Side Channel Analysis enhancement: a proposition for measurements resynchronisation" (2011) N. Debande, Y. Souissi, M. Nassar, S. Guilley, T.H. Le, J.L. DangerBakker

- "Improving differential power analysis by elastic alignment" (2011) by J.G.J. van Woudenberg, M.F. Witteman, B. Bakker
- "A general approach to power trace alignment for the assessment of side-channel resistance of hardened cryptosystems" (2012) by Q. Tian & S.A. Huss

Information retrieval from leaked data:

- "Keyboard acoustic emanations revisited" (2005) by L. Zhuang, F. Zhou, J.D. Tygar
- "Acoustic side-channel attacks on printers" (2010) by M. Backes, M. Dürmuth, S. Gerling, M. Pinkal, C. Sporleder
- "Building a side channel based disassembler" (2010) by T. Eisenbarth, C. Paar, Björn Weghenkel

- "Automated black-box detection of side-channel vulnerabilities in web applications' (2011) by P. Chapman & D. Evans
- "Current events: identifying webpages by tapping the electrical outlet" (2012) by S. S. Clark, B. A. Ransford, J. M. Sorber, W. Xu, E. G. Learned-Miller, K. Fu
- "Engineering statistical behaviors for attacking and defending covert channels" (2013) by V. Crespi, G. Cybenko, A. Giani

Conclusion

Machine learning

Retrieve meaningful information from vast amounts of leaked data.

Machine learning tools/concepts:

- Training/testing scheme
- Dimensionality reduction with PCA
- Clustering/classification with SVM
- Alignment with DTW
- Predicting/guessing usage patterns with HMM

Side channel applications

- Template based power analysis & power trace alignment
- Acoustic analysis of computer peripherals