

Full Syllabus



Course Title	
Ordinary Differential Equations 1	
Lecturer	
Arie Levant	
Semester	
A	
Course requirements	
Final grade components	
20% homework (10-12 assignments) + 80% exam	
Course schedule	
Class no. / Date	Subject and Requirements (assignments, reading materials, tasks, etc.)
	Notation. Differential (recalling). Classification of differential equations (DEs). 1st order DEs: separable, linear, Bernoulli, homogeneous, exact DE. 1st integral. Integrating factor notion. Change of variables. Systems of DE, Lotka-Volterra system.
	Cauchy problem. Vector fields. Phase space. Methods of Picard and Euler. Lipschitz condition. Theorem of the existence and uniqueness of the solution. Fixed point of a contractive mapping.
	Solution dependence on the initial conditions, the right-hand side and parameters. Solution extension. Autonomous DE. Critical points. Linearization.
	System of 1st order linear DEs. Gronwall-Bellman lemma. Solution space. Fundamental solutions. Linear dependence of functions. Wronskian.
	Systems of 1st order DEs with constant coefficients. Matrix exponent: real and complex eigenvalues, multiplicity. Exponent calculation and solution of homogeneous systems.
	High order scalar linear DEs, homogeneous and non-homogeneous. Quasi-polynomials.
	Non-homogeneous system of 1st order DEs with constant coefficients. Vector quasi- polynomials. Method of undetermined coefficients in scalar and vector cases. Method of coefficient variation. Euler equations. Abel-Liouville theorem: vector, scalar cases. Decreasing the order of DE. Solution of differential equations via power series.
	Dynamic systems, Critical points in plane. Lyapunov stability and Lyapunov functions.
	Boundary value problem. Sturm-Liouville Problem: eigenfunctions and Fourier series.
Required course reading	
Notes and other materials will be provided	
Optional course reading	
Boyce W.E. and DiPrima R.C. Elementary Differential Equations and Boundary Value Problems Arnold V.I. Ordinary Differential Equations	
Comments	

The course is taught in English.