CHAPTER 23

A Minimal Prototype for Integrating GIS and Geographic Simulation through Geographic Automata Systems

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New forms of simulation have come into popular use in geography and social science in recent years, supported by an array of advances both in the geographical sciences and in fields outside geography. These models and simulations can be characterized by a distinctly innovative approach to modeling — the geosimulation approach. Geosimulation is concerned with automata-based methodologies for simulating collectives of discrete, dynamic, and action-oriented spatial objects, combining cellular automata and multi-agent systems in a spatial context (Benenson and Torrens, 2004a, b). In geosimulation-style models, urban phenomena as a whole are considered as the outcome of the collective dynamics of multiple animate and inanimate urban objects.

Geosimulation models are more commonly based on cellular automata (CA) and multi-agent systems (MAS). Applied in isolation, CA and MAS approaches have been used to simulate a wide variety of urban phenomena and there is a natural imperative to combine these frameworks for exploratory and applied simulation in urban geography (Torrens, 2002, 2003, 2004). Nevertheless, the direct amalgamation of CA and MAS eventually suffers from awkward compromises, a function of the necessity for CA partition of urban space into cells. Given cell partition, no matter whether units are identical or vary in size and shape, cells are either granted some degree of ‘agency’ and are simply reinterpreted as artificial agents (Box, 2001) or MAS are imposed on top of CA and simulated agents respond to averaged cell conditions (Benenson, 1998; Polhill et al., 2001). These frameworks are certainly useful, especially in studying abstract models, but in a real-world milieu are a function of the limitations of the available tools rather than the structure of real urban systems or the laws of their behavior (see Agarwal, Chapter 24, this volume, for a discussion of the limitations of agent-based models).

The dataware for the real-world simulations is usually provided by Geographic Information Systems (GIS), which have an integral role in the development of geosimulation models. Dramatic changes in geographic databases during the last decades of the 20th century have ushered in a new wave of urban modeling (Benenson et al., 2002; Benenson and Omer, 2003). Automated procedures for data collection — remote sensing by spectrometer, aerial photography, scanners, video, etc. — have provided new information sources at fine resolutions, both spatial and temporal (Torrens, 2004). New methodologies for manipulating and interpreting spatial data developed by geographic information science and implemented in GIS have created added value for these data. Information collection is much more pervasive than before (Brown and Duguid, 2000), and high-resolution databases for urban land-use, population, real estate, and transport are now more widespread (Benenson and Omer, 2003). Cellular spaces populated with agents are too limiting an interface between GIS and geosimulation, and there remains much potential for fusing GIS
and geosimulation into full-blown, symbiotic simulation systems. In this chapter, we propose a minimal but sufficient framework for integrating GIS, CA, and MAS into what we term *Geographic Automata Systems* (GAS). This approach is intended to be “down to earth”, and we will demonstrate the implementation of the approach, in this chapter, with reference to GAS-based software developed at the Environment Simulation Laboratory of the Porter School of Environmental Studies at the University of Tel Aviv — the *Object-Based Environment for Urban Simulations* (OBEUS). This chapter builds on discussions of urban geocomputation (Benenson and Omer, 2000; Torrens and O’Sullivan, 2000) and software environments for geocomputational research in urban contexts (Benenson et al., 2001), which were partially presented at previous Geocomputation meetings.

### 23.2 THE BASIC AUTOMATA FRAMEWORK

Put very simply, an automaton is a processing mechanism; a discrete entity, which has some form of input and internal states. It changes states over time according to a set of rules that take information from an automaton’s own state and various inputs from outside the automaton to determine a new state in a subsequent time step. Formally, an automaton, $A$, can be represented by means of a set of states $S$ and a set of transition rules $T$.

$$A \sim (S, T)$$

(23.1)

Transition rules define an automaton’s state, $S_{t+1}$, at time step $t + 1$ depending on its state, $S_t (S_t, S_{t+1} \in S)$, and input, $I_t$, at time step $t$:

$$T: (S_t, I_t) \rightarrow S_{t+1}$$

(23.2)

Automata are discrete with respect to time and have the ability to change according to predetermined rules based on internal ($S$) and external ($I$) information.

In terms of urban applications, automata lend themselves to specification as city simulations with myriad states and transition rules. However, to make sense, an individual automaton should be as simple as possible in terms of states, transition rules, and internal information (Torrens and O’Sullivan, 2001). Simplicity is a characteristic of the most popular automata tools in urban geography, Cellular Automata — a system of spatially located and inter-connected automata.

#### 23.2.1 From General to Cellular Automata

Cellular automata are arrangements of individual automata in a partitioned space, where each unit (cell) is considered as an automaton $A$, for which input information $I$ necessary for the application of transition rules $T$ is drawn from $A$’s neighborhood $R$. In urban applications, cells are most commonly used to represent land units with state representing possible land-uses (White et al., 1997). Usually, CA lattices are partitioned as a regular square or hexagonal grid. We can specify
Equations (23.1) and (23.2) to introduce an automaton, $A$, belonging to a CA lattice as follows:

$$A \sim (S, T, R)$$

(23.3)

where $R$ denotes automata neighboring $A$.

Although there are direct analogies between land parcels and cells on the one hand and land-uses and cell states on the other, there were no geographical applications of CA models before the 1990s. There were a few examples published in the 1970s (Chapin and Weiss, 1968; Tobler, 1970, 1979; Albin, 1975; Nakajima, 1977), but the field was largely ignored in terms of research until interest was revived in the 1980s (Couclelis, 1985; Phipps, 1989). Beginning in the 1990s, CA modeling became a popular research activity in geography, with pioneering applications in urban geography (Batty et al., 1997; O’Sullivan and Torrens, 2000).

In terms of space, neighborhood relationships are important for rendering CA as spatial systems. In basic CA, neighborhoods have identical form for each automaton, for example, Moore or von Neumann (Figure 23.1A). In the last decade it became clear, however, that reliance on regular partitions of space is largely superficial in urban contexts (Torrens and O’Sullivan, 2001). Consequently, CA have been implemented on irregular networks (Figure 23.1B), or partitions given by GIS-based coverage of land parcels or Voronoi tessellations (Figure 23.1C) (Semboloni, 2000; Shi and Pang, 2000; O’Sullivan, 2001; Benenson et al., 2002). An assortment of definitions of neighborhoods, based on connectivity, adjacency, or distance can be applied to these generalized CA, where the form of the neighborhood and the number of neighbors varies between automata.

There is no conceptual difference between irregular and regular CA; yet, an inherent weakness of the CA is the inability of automata cells to move within the lattice in which they reside. Despite repeated attempts to mimic units’ mobility (Portugali et al., 1994; Schofisch and Hadeler, 1996; Wahle et al., 2001), the genuine inability to allow for automata movement in the CA framework catalyzed geographers’ recent interest in MAS. This tendency is especially strong in urban geography, where the CA framework is regarded as insufficient in dealing with mobile objects such as pedestrians (Torrens, 2004), migrating households, or relocating firms.

### 23.2.2 From General to Agent Automata

Fundamentally, agents are automata and, thus, incorporate all of the features of basic automata that have just been discussed. However, there are some important distinctions between general and agent automata, largely owing to the fact that the latter are generally interpreted for representation of autonomous decision-makers (Epstein, 1999; Kohler, 2000). In urban studies, the states $S$ of agent automata in MAS are usually designed to represent socioeconomic characteristics; transition rules are formulated as rules of agent decision-making, and correspond to human-like behaviors.

In the social sciences outside geography, work in agent-based simulation is usually non-spatial; many of the decisions and behaviors of geographic agents are, however, spatial in nature. Consequently, the states $S$ of geographic MAS should include

MINIMAL PROTOTYPE FOR INTEGRATING GIS

A

Five-cell von Neumann neighborhood

Target automaton

Eight-cell Moore neighborhood

B

Network neighbors

Automaton

Mobile automaton

Network of related automata

C

Figure 23.1 Automata defined on (A) a two-dimensional regular lattice, with von Neumann and Moore neighborhoods; (B) a two-dimensional network; (C) a Voronoi partition of two-dimensional urban space, based on property coverage.
agents’ location, and transition rules $T$ should reflect, thus, the ability of agents to relocate.

Human-based interpretations of MAS have their foundation in the work of Schelling and Sakoda (Schelling, 1969, 1971, 1974, 1978; Sakoda, 1971) and despite initial interest (Albin, 1975) the field remained relatively quiet for two decades after that. Just as with CA, the tool began to feature prominently in the geographical literature only in the mid-1990s (Portugali et al., 1997; Sanders et al., 1997; Benenson, 1999; Dijkstra et al., 2000). Until recently, the main thrust of MAS research in geography involved populating regular CA with agents of one or several kinds, which could diffuse between CA cells. Often, it is assumed that agents’ migration behavior depends on the properties of neighboring cells and neighbors (Epstein and Axtell, 1996; Portugali, 2000). Very recently, agent-based models have been designed that locate agents in relation to real-world geographic features, such as houses or roads, the latter stored as GIS layers (Benenson et al., 2002) or landscape units — pathways and view points (Gimblett, 2002).

Despite the widely acknowledged suitability of automata tools for geographic modeling (Gimblett, 2002), there has been relatively little exploration into addressing these limitations and developing patently spatial automata tools for urban simulation. In the framework described in this chapter, spatial abilities are treated with paramount importance and we define a class of automata that is capable of supporting explicit expression of processes, as geography comprehends them. In what follows, we aim at formulating a minimal framework and, thus, formulate it on the basis of an agent as an autonomous mobile object that reacts to the environmental information by changing its state and location. In terms of MAS, these agents are called weak agents and reactive agents (Woolridge and Jennings, 1995), and we assume that they are sufficient for the vast majority of high-resolution geographic applications.

### 23.2.3 What Geography Needs from Automata Systems

Focusing on space, we might identify three internal geographic mechanisms that are essential to an urban automata system:

- A typology of entities regarding their use of space in which they are situated.
- The spatial relationships between entities.
- The processes governing the changes of their location in space.

Simulating spatial systems, then, involves explicit formulation of these three components and neither CA nor MAS fully provide the necessary framework. The geography of the CA framework is problematic, for example, for urban simulation because CA are incapable of representing autonomously mobile entities. At the same time, MAS are weak as a single tool because of common underestimation of the importance of space and movement behavior.

It is evident, then, that there is a need for uniting CA and MAS formalisms in such a way as to directly reflect a geographic and object-based view of urban systems. The GAS framework that we propose attempts to satisfy that demand.
23.2.4 An Idea: Urban Object = Geographic Automaton

As a spatial science, geography concerns itself with the behavior and distribution of objects in space. In urban geography, these are urban agents — householders, pedestrians, vehicles — and urban features — land parcels, shops, roads, sidewalks, etc. In dynamic spatial systems, all these objects change their properties and/or location; the goal of a geographic model is to simulate these activities and their consequences, often at multiple scales.

In developing GAS, our aim is to infuse spatial properties into automata tools and adopt an automata-based view of urban systems. Objects are conceptualized as geographic automata, with focus on their spatial properties and behaviors. Under this framework, a city system can be modeled as an ensemble of geographic automata, that is, a GAS.

23.3 FORMAL DEFINITION OF GEOGRAPHIC AUTOMATA SYSTEMS

Geographic Automata Systems consist of interacting geographic automata of various types. In general, automata are characterized by states $S$, description of their input $I$, and transition rules $T$. In the case of geographic automata, we re-interpret and extend these components to enable the explicit consideration of space and spatial behavior.

**Specification of state set $S$:**
- In addition to non-spatial states, geographic automata are also characterized by their locations.
- Instead of the fixed location of CA automata, we introduce a set of geo-referencing rules for situating geographic automata in space.

**Specification of input information $I$:**
- Instead of relying on fixed neighborhood patterns that are incapable of being varied in space or time, we define neighborhood relations that can change in time and determine the automata providing input information for a given automaton.
- Neighborhood relations can thus change; these changes are governed by neighborhood rules.

**Specification of transition rules $T$:**
- State transition rules specify the changes of non-spatial states.
- The ability to change location is provided by a set of movement rules that allow for navigation of geographic automata in their simulated environments.

Based on these specifications, we can formulate a minimal, yet adequate, framework for geographic modeling — or geosimulation.

Let us use $K$ to denote a set of types of automata; following this we will feature each of the previously mentioned properties and rules that determine the dynamics of those automata in space. Essentially, we are constructing a system of geographic automata from the bottom-up.
The automata basis of the system is captured by a set of states $S$, associated with the GAS (consisting of subsets of states $S^k$ of automata of each type $k \in K$), and a set of state transition rules $T_S$, used to determine how automata states should change over time.

According to general definitions (23.1) and (23.2), state transitions and changes in location for geographic automata depend on automata themselves and on input ($I$), given by the states of neighbors. To specify the input information, we use $R$ to denote the neighbors of the automata and $N_R$ to specify the neighborhood transition rules that govern how automata relate to the other automata in their vicinity.

The spatial nature of the geographic automata is encapsulated by information on automata location. Let us denote this with $L$, the geo-referencing conventions employed to locate automata in the system, and $M_L$, the movement rules, governing changes in their location.

Altogether, a GAS, $G$, may be thus defined as consisting of several components:

$$G \sim \langle K, S, T_S, R, N_R, L, M_L \rangle$$ (23.4)

Let the state of geographic automaton $G$ at time $t$ be $S_t$, located at $L_t$, and the external input, $I_t$, be defined by its neighbors $R_t$. The state transition, movement, and neighborhood rules — $T_S$, $M_L$, and $N_R$ — define state, location, and input information of a given automaton $G$ at time $t + 1$ as:

$$T_S : (S_t, L_t, R_t) \rightarrow S_{t+1}$$

$$N_R : (S_t, L_t, R_t) \rightarrow R_{t+1}$$

$$M_L : (S_t, L_t, R_t) \rightarrow L_{t+1}$$ (23.5)

Exploration with GAS then becomes an issue of qualitative and quantitative investigation of the spatial and temporal behavior of $G$, given all of the components defined above. In this way, GAS models offer a framework for considering the spatially enabled interactive behavior of elementary geographic objects in a system.

### 23.3.1 Tight-Coupling between GAS and Vector GIS

Many questions arise when applying the abstract framework mentioned above to modeling specific geographic systems. Geographic automata of different types can follow different topologies. How might we incorporate that into models: let householders react to their neighbors in the adjacent houses (irregular tessellation); drivers to cars ahead, behind, and on their sides (point events on the network); customers to shops, which can be far away (graphs)? How could automata represent continuous fields, if ever? How can theoretical ideas relating to spatial mobility — way-finding, spatial cognition, action-at-a-distance, etc. — be incorporated into the behavioral rules of the real-world mobile agents or immobile features and further translated into automation rules? How can the global patterns reflecting self-organization of non-elementary urban entities be recognized and validated if generated in simulations?
Answering these questions requires a tight-coupling between GIS and automata-based models.

As a first step, we could rely on vector GIS. Indeed, vector GIS as a special kind of Database Management System (DBMS). Indeed, vector GIS may provide much support for GAS models. First and foremost, vector GIS can be used to store and retrieve the location and states of spatial objects and to register spatial actions. The next step toward fusion of GIS and geosimulation exploits an object-based view of urban reality. Indeed, both GAS and vector GIS are object-based in their design; both deal with discrete spatial objects, which customarily represent the real world at “microscopic” scales. A geosimulation approach considers the city as a dynamic collective of spatially located objects. Vector GIS deals mostly with static objects and employs an entity-relationship model (ERM) for their representation. In our approaches detailed here, we merge GAS and vector GIS functionality by implementing GAS as a specialized object-oriented database that manages geographic automata. Automata of a certain type are interpreted as a class, states and location as class properties; and GAS state transition, movement and neighborhood transition rules of automata of different types are thus reformulated as methods of corresponding automata classes. Let us specify components of GAS definition (23.4) and (23.5).

### 23.3.2 Geographic Automata Types, \( K \)

At an abstract level, we distinguish between fixed and non-fixed geographic automata. Fixed geographic automata represent objects that do not change their location over time and, thus, have close analogies with CA cells. In the context of urban systems, these are objects such as road links, building footprints, parks, etc. Fixed geographic automata may be subject to state and neighborhood transition rules \( TS \) and \( NR \), but not of rules of motion, \( ML \).

Non-fixed geographic automata symbolize entities that change their location over time, for example: pedestrians, vehicles, and households. The full range of rules for GAS can be applied to non-fixed geographic automata.

Geographic automata of either fixed or non-fixed type evidently correspond to vector GIS features; normally the automata of a given type correspond to the features of a certain layer of vector GIS.

### 23.3.3 Geographic Automata States and State Transition Rules, \( S \) and \( TS \)

State transition rules \( TS \) are based on geographic automata of all types from \( K \). In contrast to CA, the states \( S \) of urban fixed infrastructure objects depend on the neighboring objects of the infrastructure, but are also driven by non-fixed geographic automata — agents — that may be responsible for governing object states such as land-use, land value, etc. In this way, urban objects do not simply mutate like bacteria (O’Sullivan and Torrens, 2000); rather, state transition is governed by other objects, the latter crucial for simulating human-driven urban systems, in which people are affected by their environments and also change them.
Interpreted in GIS terms, automaton states are attribute values of a corresponding GIS feature, while state transition rules exploit attributes of GIS features that are in spatial and non-spatial relationships with a given automaton.

### 23.3.4 Geo-Referencing Conventions, \( L \) and Movement Rules \( M_L \)

Geo-referencing conventions are crucial for coupling GAS and GIS. On the one hand, they should be sufficiently flexible to enable translation of geographic perspectives on locating real world objects, both fixed and non-fixed; on the other, they should satisfy limitations of ERMs, in order to be convenient for GIS management.

The GAS framework resolves these limitations by introducing two forms of geo-referencing — direct and by pointing. Direct methods of geo-referencing follow a vector GIS approach for representing reality, using coordinate lists. Such a list indicates all spatial details necessary to represent an object — automata boundaries, centroids, nodes’ location, etc. Fixed geographic automata are usually located by means of direct geo-referencing. The details of the particular rules employed depend on the automata used in a modeling exercise. For typical urban objects such as buildings or street segments, two-dimensional footprint polygons or three-dimensional prisms may be used.

Non-fixed geographic automata may move; updating position coordinates might cause difficulties, which, when the automata are numerous and their shape is complex, are irresolvable in the framework of an ERM. We address these difficulties with a second method of geo-referencing — by pointing to other automata (Figure 23.2).

Let us consider a typical example. In the case of property dynamics, householders can be geo-referenced by address. Landlords provide a more complex case: they can be geo-referenced by pointing to the properties that they own. Indirect referencing can also be used for fixed geographic automata, for example, for apartments in a house (Torrens, 2001). Referencing by pointing is dynamic-enabled both in space and in time and compatible with the ERM database model.

![Figure 23.2](image)  
**Figure 23.2** Direct and indirect geo-referencing of fixed and non-fixed GA.
GAS-based research into different formulations of $M_L$ offers great potential for geographers. Realistic rules, $M_L$, for encoding automata movement, based on repel–attract–synchronize interactions between close neighbors, are being developed, for example, in Animat research (Meyer et al., 2000) and in the gaming industry (Reynolds, 1999). There is much opportunity for geographers to contribute to this line of research. Traditionally, attention has focused on the generation of realistic choreographies for automata, particularly in traffic models, through the specification of rules for collision avoidance, obstacle negotiation, lane-changing, flocking, behavior at junctions, etc. (Torrens, 2004). However, there remain many relatively neglected areas of inquiry: spatial cognition, migration, way finding, navigation, etc.

23.3.5 Neighbors and Neighborhood Rules, $R$ and $N_R$

The set of neighbors of automata, $R$, is necessary for determining input information $I$. In contrast to the static and symmetrical neighborhoods usually employed in CA models (Figure 23.1A), spatial relationships between geographic automata can vary in space and time, and, thus, rules for determining neighborhood relationships $N_R$ is necessary. Neighborhood rules for fixed geographic objects are relatively easy to define (simply because the objects are static in space). There are a variety of geographical ways in which neighborhood rules can be expressed for them — via adjacency of units in regular or irregular tessellations, connectivity of network nodes, proximity, etc. (Figure 23.1B, C), all fit naturally in the context of GIS operations. Spatial notions related to the incorporation of human-like automata into GAS, such as accessibility, visibility, and mental maps can be formally encoded as $N_R$ rules.

Non-fixed geographic automata pose more of a challenge when specifying neighborhood rules, because the objects — and hence their neighborhood relations — are dynamic in space and time. It can be done straightforwardly, via distance and nearest-neighbor relations, as used in Boids models (Reynolds, 1987), but as movement rules $M_L$. This can become very heavy computationally when complex definition of, say, visibility or accessibility is involved. In this case, it is more appropriate to base neighborhood rules on indirect location, as defined in previous sections, and consider two indirectly located automata as neighbors when the automata they point to are neighbors.

For example, two householder agents can be established as neighbors by assessing the neighborhood relationship between the houses in which they reside. Even when these agents are physically separated in the simulation — when they go shopping or go to work, for example — they remain “neighbors” by virtue of the (fixed) relationship between their properties.

23.3.6 Temporal Dimension of GAS

A methodological base composed of fixed and non-fixed objects and direct and by-pointing locating implies specification of GASs within GIS. However, the dynamic nature of GAS also implicates temporal dimensions of GIS databases, and, thus entails its own limitations. Given these considerations, transition rules $T_S$, $M_L$, and $N_R$. 
should be defined in a way that avoids conflicts when geographic automata are created or destroyed and their states, locations, or neighborhood relations are updated.

According to (5), a triplet of transition rules determines the states $S$, locations $L$, and neighbors $R$ of automata at time $t + 1$ based on their values at time $t$. It is well known that different interpretations of the “hidden” — time — variable in a discrete system can critically influence resulting dynamics of the model (Liu and Andersson, 2004). There are several ways to implement time in a dynamic system. On the one hand, we consider time as governed by an external clock, which commands simultaneous application of rules (5) to each automaton at each tick of the clock. On the other hand, each automaton can have its own internal clock and, thus, the units of time in (5) can have different meaning for different automata. Formally, these approaches are expressed as Synchronous or Asynchronous modes of updating of automata states and location. System dynamics depend strongly on the details of the mode employed (Berec, 2002; Liu and Andersson, 2004), and the spatial aspects of the problem are studied in temporal GIS (Miller, 1999; Peuquet, 2002). Tight coupling between GAS and GIS might thus demand further development of temporal GIS.

23.3.7 GAS and Raster GIS

Conceptually, GAS do not fit to modeling dynamics of continuous fields, as, say, erosion processes, or pollution transport. Nonetheless, it is formally easy to interpret raster GIS cells as geographic automata, if the resolution is established a priori. It is also worth noting that in the majority of situations the sources and recipients of continuously distributed characteristics are geographic automata. One can think about further coupling between GAS and continuous models, but such an extension is merely beyond the minimal framework we discuss.

23.4 THE SOFTWARE IMPLEMENTATION OF GAS

A software implementation of GAS for urban modeling — OBEUS — is currently in development at the Environment Simulation Laboratory of the University of Tel Aviv (Benenson et al., 2001, 2004). Recently, OBEUS was modified to include all the basic characteristics of GAS, and that was intentionally done in a minimal possible manner. Based on recent OBEUS experience, we specify — below — the main components that are necessary to implement the GAS approach as a software environment. The shareware version of OBEUS is still in development and is planned for distribution in April 2004 (see http://eslab.tau.ac.il for updates). The GAS framework is not software-or language-specific, however, and applications have been developed in different environments (Torrens, 2003).

23.4.1 Abstract Classes of OBEUS

The basic components of GAS are defined in OBEUS with respect to automata types $k \in K$, its states $S_k$, location $L$, and neighborhood relations $R$ to other objects. These
are implemented by means of the two-level structure of abstract root classes presented, partially, in Figure 23.3.

At the top level we define three abstract classes: Population contains information regarding the population of objects of given type k as a whole; GeoAutomata acts as a container for geographic automata of specific type; GeoRelationship facilitates specification of (spatial, but not necessarily) relationships between geographic automata. This functionality is available regardless of the degree of neighborhood and other relationships between automata, whether they are one-to-one, one-to-many, or many-to-many.

The location information for geographic automata essentially depends on whether the object we consider is fixed or non-fixed. This dichotomy is handled using abstract classes, Estate and Agent, which inherit GeoAutomata. The Estate class is used to represent fixed geographic automata. The Agent class represents non-fixed geographic automata.

Following from GeoRelationship, three abstract relationship classes can be specified: EstateEstate, AgentEstate, and AgentAgent. The latter is not implemented in order to avoid conflicts in relationship updating (see Section 23.4.3 below), and the only way of locating non-fixed agents modeled in OBEUS is by pointing to fixed estates; consequently, direct relationships between non-fixed objects are not allowed. This might limit possible applications of the system — we already mentioned the boids model (Reynolds, 1999) as an example where direct Agent–Agent relationships are necessary. At the same time, the majority of urban models we are aware of do not need them, and most examples in which Agent–Agent relationships are important arise in contexts beyond the intuitive limitations of the “reactive agent” idea; marriage is one example that a reviewer of this chapter suggested.

### 23.4.2 Management of Time in OBEUS

The OBEUS architecture utilizes both Synchronous and Asynchronous modes of update. In Synchronous mode, all automata are assumed to change simultaneously and conflicts can arise when agents compete over limited resources, as in the case of two householders trying to occupy the same apartment. Resolution of these conflicts depends on the model’s context, a decision OBEUS leaves to the modeler. In Asynchronous mode, automata change in sequence, with each observing a geographic reality left by the previous automata. Conflicts between automata are thereby resolved; but the order of updating is critical as it may influence results.

OBEUS demands that the modeler sets up an order of automata update according to a template: randomly, sequence in order of some characteristic, and object-driven approaches are currently being implemented.

### 23.4.3 Management of Relationships in OBEUS

Relationships in GAS models can change in time and this might cause conflicts, when, in housing applications, for example, a landlord wants to sell his property, while the tenant does not want to leave the apartment. This example represents the
Figure 23.3 A UML scheme illustrating the abstract-level classes of OBEUS and the example of model-level classes for a residential dynamics simulation.
general problem of consistency in managing relationships. It has no single general solution; there are plenty of complex examples discussed in the computer science literature (Peckham et al., 1995). OBEUS aims at minimal representation of the GAS framework and thus follows the leader–follower development pattern proposed by Noble (2000). To maintain consistency in relationships, an object on one side, termed the leader, is responsible for managing the relationship. The other side, the follower, is comprised of passive objects. The leader provides an interface for managing the relationship, and invokes the followers when necessary. There is no need to establish leader or follower “roles” in a relationship between fixed objects once the relationship is established, while in relationships between a non-fixed and a fixed object, the non-fixed object is always the leader and is responsible for creating and updating the relationship. For instance, in a relationship between a landlord and her property (when ownership cannot be shared), the landlord initiates the relationship and is able to change it. We do not have evidence that the majority of real-world situations can be imitated using a leader–follower pattern, but we are also unaware of cases — in urban contexts — where this pattern would be insufficient.

23.4.4 Implementing System Theory Demands within OBEUS

Systems theory suggests another challenge for automata modeling in which the usefulness of the GAS–OBEUS approach appears to offer advantages. In a systems context, many interacting automata are often necessary for capturing the nuances of geographic reality. It is very well known that if system rules are non-linear and the system is open, then emergence and self-maintenance of entities at above-automata levels become feasible. Gentrified areas and commuting zones are examples.

The idea of self-organization is external to GAS and it is not necessary to incorporate it into the software implementation. Nonetheless, self-organization is often too important for studying urban systems to be ignored, even at the first step of GAS software implementation. To accommodate this, emerging spatial ensembles of geographic automata are supported in OBEUS by means of the abstract class GeoDomain. The simplest approach to emergence, determined by the set of a priori given predicates defined on geographic automata is implemented; domains are thus limited to capturing ‘foreseeable’ self-organization of specific types.

As with non-fixed agents, domains are always leaders in their relationships with the automata within them. These relationships can capture properties such as distance between fixed automata and the domain; several definitions of distance based on objects’ and domains’ centroids, boundaries, etc. can be applied.

23.4.5 Example of GAS Modeling Style — the Schelling Model in Terms of OBEUS

The well-known Schelling model of residential dynamics (Schelling, 1971; Hegelsmann and Flache, 1998) reflects a basic idea of residential segregation between the members of two mutually avoiding population groups, as a self-organizing phenomenon. Thomas Schelling realized his model with black and white checkers...
on a chess-board and from then on, the model is formulated in terms of agents of two types, B and W, located in the cells of a regular grid, with a maximum of one agent per cell. The essence of the Schelling model is in assumption that if the fraction of agents of strange type (say, of W-type for the B-agent) within the neighborhood of a current agent’s location is above the tolerance threshold of an agent, then an agent tries to relocate to a nearest unoccupied location, where the fraction of strange agents is below that threshold. The Schelling model is asynchronous and each agent observes the state of the system as left by the previous one.

As an applied example of GAS, let us formulate this model in GAS terms and then present the entities and methods necessary to implement it in OBEUS.

Two **types** of objects ($K = 2$) **Fixed Objects**: Cells C;

- Cell states $S$:
  - Cells have no states, i.e., $S_1 = \emptyset$;
- Cell location rules $L$:
  - Each cell $C$ is assigned a pair of coordinates $(x, y)$ for direct location,
    $L_1 = \{\text{Locate } C(x, y) \text{ at } (x, y)\}$;
- Neighborhood rules $R$ (Moore, as an example):
  - $R_1 = \{\text{For a cell } C(x, y), \text{ cells } B(u, v), \text{ given max}(|u - x|, |v - y|) = 1 \text{ are neighbors}\}$;
- State transition rules $T$:
  - None, i.e., $T_1 = \emptyset$;
- Movement rules $M$:
  - None, $M_1 = \emptyset$, there are no movement rules for fixed objects;
- Neighborhood transition rules $N$:
  - None, $N_1 = \emptyset$, neighborhood relations of fixed objects do not change.

**Non-Fixed Objects**: Residents D,

- Resident states $S$:
  - Resident can be in one of two states, B or W, $S_2 = \{B, W\}$
- Resident location rules $L$:
  - Resident is located indirectly, by pointing to a cell it occupies, $R_2 = \{\text{Cell } C\}$
- Neighborhood rules $R$:
  - $R_2 = \{\text{Residents located in neighboring cells are neighbors}\}$
State transition rules T:
None, \( T_2 = \emptyset \);

Neighborhood transition rules N:
None, \( N_2 = \emptyset \).

Movement rules (one of the versions) M:
\[ M_2 = \{ \text{If fraction of strangers } f_R \text{ among the neighbors is below threshold, i.e., } f_R < f_{TH}, \text{ do nothing; otherwise find the closest unoccupied cell satisfying } f_R < f_{TH} \text{ and relocate there; if there is more than one at the same distance choose one among them randomly; if no suitable location is found do nothing} \} \]

The OBEUS implementation of the “Schelling” GAS is as follows (Figure 23.3):

1. The abstract classes \textit{Agent} and \textit{Estate} are inherited by \textit{Resident} and \textit{Cell}, respectively.
2. The abstract relationship classes \textit{EstateEstate} and \textit{AgentEstate} are inherited by \textit{CellCell} and \textit{ResidentCell}, respectively.
3. Class \textit{Cell} has no properties of its own.
4. Class \textit{Cell} has one basic method of its own \texttt{getEmptyCloseCells(distance, cell)} which employs \texttt{getRelatedEstates(estate)} and returns the list of non-occupied neighboring cells at a distance \textit{distance}.
5. Class \textit{Resident} has two properties of its own — Boolean \textit{color}, with values B and W, and real \textit{Tolerance} threshold.
6. Class \textit{Resident} has two basic methods of its own, \texttt{getFriends(resident, cell)} and \texttt{getStrangers(resident, cell)}, which employ \texttt{getRelatedEstates(estate)}, and return lists of the neighbors of the color which is same or opposite to the color of a resident if located in a cell \textit{cell}.

The goal of the Schelling GAS is to study residential segregation and, thus, its investigation demands recognition of areas populated mostly or exclusively by B- or W-agents. This can be done by specifying domain criteria based on the \textit{CellCell} and \textit{ResidentCell} relationship. Namely, let us consider a cell \textit{C} occupied by resident \textit{R} of a color \textit{L}. Let us define the cell \textit{C} as \textit{S}_L\text{-true} (segregation-true of a color \textit{L}) if the fraction of resident’s neighbors of color \textit{L} is above the given threshold \textit{f}. For the Schelling model, if we take the value of \textit{f} high enough (and higher than the tolerance threshold of residents), the sets of \textit{S}_L\text{-true} cells for \textit{L} = B and \textit{L} = W will form continuous areas that reflect intuitive understanding of segregation. The value of \textit{f} determines the density of the residents of the same color in the domain and the degree of the overlap of \textit{S}_B and \textit{S}_W domains. The concept of domains is considered in more details in (Benenson et al., 2004) and it is beyond the scope of this chapter. Let us note, however, that we consider the formulation of domain criteria and investigation the patterns produced by the geographic automata that satisfy the criteria as a necessary step in understanding spatial patterns that can emerge in the model.
23.5 CONCLUSIONS

We have introduced a GAS framework as a unified scheme for representing discrete geographic systems. Technically, the framework is designed to merge two popular tools used in urban simulation — CA and MAS — and specify them in a patently spatial manner. Conceptually, our assertion is that GAS forms the kernel of the system, as far as the system is spatially driven.

The minimal GAS skeleton allows for a degree of standardization between automata models and GIS. It also provides a mechanism for transferability. Until now, the majority of spatial simulations can be investigated only by their developers. The development of GAS software breaches this barrier, offering opportunities to turn urban modeling from art into engineering.

A few additional steps are necessary for full implementation of the GAS framework; none, we think, requires decades of research to realize. The first requirement we have identified relates to transforming the GAS framework into software. As demonstrated with reference to OBEUS, we have advanced along that line of research inquiry, in urban contexts. Development of a (preferably geography-specific) simulation language based on GAS is a second requirement that we consider. The intent, in that context, is to enable the formulation of simulation rules in terms of objects’ spatial behavior. We believe that the continued development of simulation languages (Schumacher, 2001) that has gathered steam in the last decade, coupled with advances in GI Science and spatial ontology, could answer this requirement in the near future. The third requirement is development of GAS applications. We have developed GAS-based models of housing dynamics (Benenson et al., 2002) and urban growth (Torrens, 2002, 2003) thus far, and the results are promising.

REFERENCES


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