

Smooth Functions

$f(\mathbf{x})$	$\text{dom}(f)$	parameter	norm
$\frac{1}{2}\mathbf{x}^T \mathbf{A}\mathbf{x} + \mathbf{b}^T \mathbf{x} + c$ $(\mathbf{A} \in \mathbb{S}^n, \mathbf{b} \in \mathbb{R}^n, c \in \mathbb{R})$	\mathbb{R}^n	$\ \mathbf{A}\ _{p,q}$	l_p
$\langle \mathbf{b}, \mathbf{x} \rangle + c$ $(\mathbf{b} \in \mathbb{E}^*, c \in \mathbb{R})$	\mathbb{E}	0	any norm
$\frac{1}{2}\ \mathbf{x}\ _p^2, p \in [2, \infty)$	\mathbb{R}^n	$p - 1$	l_p
$\sqrt{1 + \ \mathbf{x}\ _2^2}$	\mathbb{R}^n	1	l_2
$\log(\sum_{i=1}^n e^{x_i})$	\mathbb{R}^n	1	l_2, l_∞
$\frac{1}{2}d_C^2(\mathbf{x})$ $(\emptyset \neq C \subseteq \mathbb{E} \text{ closed convex})$	\mathbb{E}	1	Euclidean
$\frac{1}{2}\ \mathbf{x}\ ^2 - \frac{1}{2}d_C^2(\mathbf{x})$ $(\emptyset \neq C \subseteq \mathbb{E} \text{ closed convex})$	\mathbb{E}	1	Euclidean
$H_\mu(\mathbf{x}) (\mu > 0)$	\mathbb{E}	$\frac{1}{\mu}$	Euclidean

Strongly Convex Functions

$f(\mathbf{x})$	$\text{dom}(f)$	s.c. parameter	norm
$\frac{1}{2}\mathbf{x}^T \mathbf{A}\mathbf{x} + 2\mathbf{b}^T \mathbf{x} + c$ $(\mathbf{A} \in \mathbb{S}_{++}^n, \mathbf{b} \in \mathbb{R}^n, c \in \mathbb{R})$	\mathbb{R}^n	$\lambda_{\min}(\mathbf{A})$	l_2
$\frac{1}{2}\ \mathbf{x}\ ^2 + \delta_C(\mathbf{x})$ $(\emptyset \neq C \subseteq \mathbb{E} \text{ convex})$	C	1	Euclidean
$-\sqrt{1 - \ \mathbf{x}\ _2^2}$	$B_{\ \cdot\ _2}[\mathbf{0}, 1]$	1	l_2
$\frac{1}{2}\ \mathbf{x}\ _p^2 (p \in (1, 2])$	\mathbb{R}^n	$p - 1$	l_p
$\sum_{i=1}^n x_i \log x_i$	Δ_n	1	l_2 or l_1