## 4.4.2016

- 9. For a 1+1 and 2+1 dimensional spacetimes, consider a general coordinate transformation. Expand (as in class) the metric to the second order in a Taylor series. How many degrees of freedom at each spacetime point describe here curvature.
  - 10. Show that the Christoffel "symbol" is not a tensor.
  - 11.  $ds^2 = (1 + A(r))dt^2 r^2(dr^2 + \sin^2(\theta)d\phi^2).$

Calculate the Christoffel matrix and the geodesic equations for massive and massless particles.

12. Suppose  $P_{\lambda\mu\nu}$ , is such that  $A^{\lambda}P_{\lambda\mu\nu}$ , is a tensor for any vector  $A^{\lambda}$ . Then  $P_{\lambda\mu\nu}$  is a tensor.