

Kantor, Kardar, and Nelson Reply: Recently we reported some results on statistical mechanics of two-dimensional networks.¹ Because of entropy effects, a self-avoiding manifold assumes a typical radius R that grows with its linear size L as $R \sim L^\nu$. Monte Carlo simulations in three dimensions lead to $\nu \sim 0.8$ in good agreement with a Flory estimate of $\frac{4}{5}$. For strips of width w and length L , we suggested a scaling form $R \sim (wL^3)^{1/5}$ which interpolates between $R \sim L^{4/5}$ for $w \sim L$ and $R \sim L^{3/5}$ for $w \ll L$. Note that $\frac{3}{5}$ is the Flory estimate for a *free polymer* in 3D. The crumpled balls obtained by crushing strips of paper^{2,3} are *nonequilibrium* configurations that belong to an ensemble entirely different from the equilibrium ones mentioned earlier. Here we briefly remark on similarities and differences between these two ensembles, and present a simple explanation for the experimental results of the preceding Comment.³

Consider a D -dimensional manifold ($D=1$ for polymers, and $D=2$ for surfaces) crumpled under strong pressure in d dimensions. If the network collapses to a compact object whose fractal dimension equals the dimension d of space, the radius grows as $R \sim L^{\nu_c}$ with $\nu_c = D/d$ (since mass $\sim L^D \sim R^d$). A string of length L can easily be compacted in this fashion into a ball of radius $R \sim L^{\nu_c - 1/3}$ in $d=3$. It is, however, much more difficult for *surfaces* to achieve this compaction without tearing.⁴ This is why crumpled aluminum foils¹ and crushed pieces of paper^{2,3} result in a nontrivial exponent $\nu_2 \approx 0.8 > \frac{2}{3}$. The interior of a crushed paper ball (seen by gently opening the ball) looks rather similar to pictures of free surfaces from Monte Carlo simulations, which may account for the similarity in the exponent ν for the two systems.

For the compacted strips of length L and width w studied by Gomes and Vasconcelos,³ we would expect $R \sim w^\alpha L^\beta$ with an exponent that interpolates between compacted strings ($R \sim L^{1/3}$) for $L \gg w$, and crushed surfaces ($R \sim L^{\nu_2 - 0.8}$) for $L \sim w$. This leads to the conclusion $\alpha = \frac{1}{3} \sim 0.33$ and $\beta = \nu_2 - \frac{1}{3} \sim 0.47$. These ex-

ponents are quite consistent with the results reported in the preceding Comment.³ Indeed, that agreement seems to improve for samples including a larger range of L/w , and hence more likely to be compacted to a uniform density.

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¹Y. Kantor, M. Kardar, and D. R. Nelson, Phys. Rev. Lett. **57**, 791 (1986), and Phys. Rev. A **35**, 3056 (1987).

²M. A. F. Gomes, J. Phys. A **20**, L283 (1987).

³M. A. F. Gomes and G. L. Vasconcelos, preceding Comment [Phys. Rev. Lett. **60**, 237 (1988)].

⁴As discussed in Ref. 1, it is very difficult to "intelligently" fold a quasi-isometric self-avoiding surface into a compact object. We are familiar with only one such procedure, due to R. C. Ball (unpublished).