Writer Identification in Modern and Historical Documents via Binary Pixel Patterns, Kolmogorov–Smirnov Test and Fisher's Method

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Abstract. The authors present a new method of writer identification, employing the full power of multiple experiments, which yields a statistically significant result. Each individual binarized and segmented character is represented as a histogram of 512 binary pixel patterns— 3×3 black and white patches. In the process of comparing two given inscriptions under a "single author" assumption, the algorithm performs a Kolmogorov–Smirnov test for each letter and each patch. The resulting p-values are combined using Fisher's method, producing a single p-value. Experiments on both Modern and Ancient Hebrew data sets demonstrate the excellent performance and robustness of this approach. © 2017 Society for Imaging Science and Technology.

INTRODUCTION

The current article deals with the challenging task of writer identification in historical documents. In what follows, we provide a short overview of the existing approaches to this task, and present the main contribution of this article.

Prior Work

The problem of computerized writer identification within historical documents exists in the literature for several decades.¹ Several features and their combination methods have been proposed for that purpose. The article Ref. 1 uses run-length histograms, combined via PCA (first two components). Article Ref. 2 continues the use of run-length distributions, supplementing them with allographic features (grapheme codebook generated using self-organizing map); the feature fusion is performed via simple or weighted averaging distances due to the individual features. Similar allographic features ("fraglets"), optionally supplemented with edge-directional feature ("hinge") are present in Ref. 3, with Hamming distance measures between the normalized features.

The article Ref. 4 presents another feature combination technique; extracting 8 types of features pertaining to various relations between foreground and background pixels of segmented characters, as well as their central moments. The features are selected via dimension reduction techniques such as sequential forward floating selection and linear discriminant analysis, classifying the reduced feature vectors via a linear Bayes classifier or K-nearest neighbors. Yet another set of classifiers based on grid microstructure, allograph level and topological features, combined via weighting procedure, is presented in Ref. 5. Article Ref. 6 provides a wealth of contour-based, oriented basic image, as well as SIFT, features classified by a voting procedure and SVM; Ref. 7 uses a similar setup, adding HOG features. An adaptation of SIFT features is also used in Ref. 8, with dimensionality reduced via PCA, resulting in a visual vocabulary. The features are clustered using a Gaussian Mixture Model and employing the Fisher kernel. A recent use of KDA in a setting involving both chain-code and edge-based directional features can be found in Ref. 9.

A thoroughly different approach is demonstrated in Ref. 10, operating on a segmented character level, and treating them as realizations of estimated "Ideal Prototypes." The identity or distinction among writers is made via several techniques, employing comparisons of the contours of the realizations to various ideals, and using heuristics and maximum likelihood estimations procedure combining information from different letters in order to find similar writers. A similar method is described in Ref. 11, with comparisons between character or ideal contours solved analytically.

A review of these articles, as well as surveys of the broader field of writer identification,^{12,13} demonstrate the common denominators of most of these algorithms: a series of features (e.g., based on edge, allograph or topological information, or using "classical" computer vision features such as SIFT, HOG and Gabor filters) is extracted. Optionally, the dimensionality is reduced (e.g., via weighting, LDA, PCA or KDA methods), followed by writer classification of the resulting feature vectors (e.g., by employing KNN, SVM, MLE or the Fisher Kernel). Usually, the question is whether a given document, according to some metric, is written by the same author as the most closely matching document. Alternatively, several (e.g., 5 or 10) "closest" documents are fetched for the purpose of identifying at least one identical writer. The algorithm's performance is checked based on an existing ground truth.

Although some of these methods perform reasonably for their tasks and data sets, their typical output is an

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abstract distance between two given inscriptions, or else a table indicating the distances between several inscriptions. However, these distances do not yield any probabilistic information. Thus, it is difficult to interpret such an output outside a well ground-truthed framework. In particular the distances, by themselves, are insufficient for the different task of analyzing a corpus of many inscriptions, with an unknown number of authors.

The existing approaches can be contrasted with the direct predecessor of this article,¹⁴ which proposes a statistical approach. The article used a sophisticated concatenation and subsequent combination of SIFT, Zernike, DCT, and K_d -tree, image projections, CMI¹⁵⁻¹⁷ and L_1 features and distances. Subsequently, on an inscriptions' pair-wise basis, the writer identification analysis was performed independently for each letter. This resulted in different statistical *p*-values, estimating the probability of a single author producing the different letter instances of the two inscriptions. These independent *p*-values were later combined into a "meta" p-value via Fisher's Method (a brief explanation is provided below), typically resulting in more significant results. Contrary to the existing approaches, such an approach can be easily utilized in order to detect different authors within any given corpus, by detecting "meta" *p*-values below certain threshold.

Finally, we rely on previously developed document preprocessing techniques. In particular, we assume the existence of a suitable binarization, segmentation and (if needed) restoration of characters, whose quality is suitable for our needs. The inputs for the described method are individual black and white images of single characters, reflecting the original writing as reliably as possible (e.g., not thinned, no slant correction, etc.). Such automatic or semimanual techniques are described, for our data sets, in Refs. 17–19 and especially in Refs. 14, 20; for other approaches, consult the references mentioned in Ref. 4, 10, 11. For methods assessing the adherence of character's reconstruction to its image, as well as the general quality of the resulting binarization, see Refs. 15, 16, 21, 22. Additional details regarding the preparation of the different data sets are provided below.

The Main Contribution of this Article

In this research, we advance the ideas of Ref. 14 to the next level. The analysis is performed independently, not only on a level of a single letter, but also on the level of a single feature, unleashing the full statistical power of multiple experiments. The main changes from Ref. 14 are: an entirely different, and much larger set of features (using 512 different binary pixel patterns instead of a combination of 7 features); a two-step experimental process, working on both individual feature (by comparing the feature distributions via Kolmogorov–Smirnov test), as well as individual letter level in order to deduce the *p*-values, later to be combined via Fisher's method (potentially, thousands of experiments, equaling the number of letters multiplied by the number of features, are conducted!); and an improvement in the significance level of the results by lowering the

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p-value threshold. All these allow us to establish a robust platform for analyzing corpora of many inscriptions, with an unknown number of authors, while arriving at meaningful and statistically highly significant outcomes. A schematic comparison of the various handwriting analysis schemes is presented in Figure 1.

ALGORITHM'S DESCRIPTION *Preliminary Remarks*

We use the common statistical convention of defining a "null hypothesis" H_0 and trying to *disprove* it. In our case, H_0 is "two given inscriptions were written by the same author." The probability for this event is the *p*-value, which will be estimated via the algorithm. If the *p*-value is *lower* than a pre-defined threshold, H_0 is rejected, and the competing hypothesis of "two different authors" is declared valid. On the other hand, an inability to reject the null hypothesis does not indicate its validity. In such a case we remain agnostic, not being able to say anything regarding the documents' authors.

The estimation of the *p*-value involves an activation of the Kolmogorov–Smirnov (KS) test, a classical nonparametric test, allowing for a comparison of two samples, not necessarily of the same size.²³ The main idea of KS is a comparison of *the empirical* distribution functions F_1 and F_2 (produced from the two samples), in order to calculate the observed statistic $D = \sup_x |F_1(x) - F_2(x)|$. The *p*-value of this statistic, under the hypothesis that the two samples stem from the same distribution, can be either calculated directly (via permutations) or approximated (our research utilizes the implementation²⁴). For example, if the samples' sizes are large enough, and all the values within the first sample are smaller than the values of the second sample, the *p*-value should be low. A previous usage of Kolmogorov–Smirnov test in a signature verification setting can be seen in Ref. 25.

Another well-established technique used by the algorithm is Fisher's method for *p*-value combinations.²⁶ Given *p*-values p_i (i = 1, ..., k) stemming from k independent experiments, the method allows one to estimate a combined pvalue, reflecting the entire wealth of evidence at our disposal. The method utilizes the fact that $X_{2k}^2 \sim -2 \sum_{i=1}^k \ln(p_i)$, i.e., the sum produces a chi-squared distribution with 2k degrees of freedom. This allows for a calculation of a single combined ("meta") p-value. Intuitively, if several experiments produce low *p*-values (e.g., 0.1, 0.15 and 0.2), the probability for such an occurrence, by chance, is very small, and the combined p-value will also be low (possibly even lower than the original *p*-values; 0.071 for the last example). However, in the current article, the *p*-values of multiple experiments (stemming from different characters and features) are not necessarily independent, but are expected to be positively correlated. Thus, we are "overconfident" in the combined evidence against H_0 . A common remedy to this problem is to demand more significant results, by substituting T with $T \cdot (k+1)/2k$ (k is the number of experiments), a common modification representing a mean of false discovery rates.²⁷ In our case, this demand can be satisfied simply by lowering

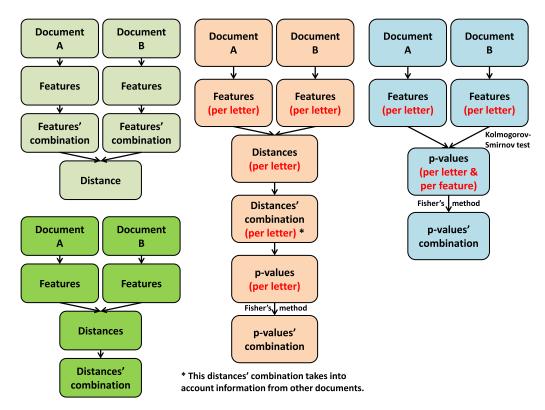


Figure 1. A comparison of handwriting analysis schemes. Left: common frameworks, producing an *abstract distance* between the documents as a final output. Center: the method of Ref. 14, performing the analysis on per-letter basis, yielding (number of letters) experimental *p-values* to be combined via Fisher's method. Right: the current technique, performing Kolmogorov–Smirnov tests for each feature and each letter, yielding (number of features) x (number of letters) experimental *p-values* to be combined via Fisher's method.

the threshold *p*-value *T* from 0.2 (as in Ref. 14) to 0.1 or even 0.05.

Prior Assumptions

We begin with two images of different inscriptions, denoted as *I* and *J*. The algorithm operates based on information derived at a character level. Herein, by a character we denote a particular instance of a given letter (e.g., there may be many characters, which are all instances of a letter *alep*). As remarked above, we assume that the inscriptions' characters are binarized and segmented into images I_{il}^l ($i_l = 1, ..., M_l$, representing the instances of the letter *l* within *I*); and J_{jl}^l ($j_l = 1, ..., N_l$, representing the instances of the same letter *l* within *J*), belonging to appropriate letters (l = 1, ..., L). In the current research, the binarization and segmentation was performed automatically for Modern Hebrew, and in semimanual fashion for Ancient Hebrew documents.^{14,20} The resulting characters' images were padded with a 1-pixel white border on each side.

Histogram Creation for each Character

Our features are the 3 × 3 binary pixel patterns, i.e., image patches of the individual characters (for additional information on pixel patterns, see the examples in Refs. 28, 29). There are $2^9 = 512$ optional patches of that size. All such possible patches are extracted from the images I_{il}^l and J_{il}^l , in order to create normalized patches' histograms (counting frequencies of patches' occurrences), $H_{i_l}^l(p)$ and $G_{i_l}^l(p)$, respectively (p = 1, ..., 512).

A simple, yet illustrative, example of two such images and their respective histograms is seen in Table I. Remarkably, despite a similar overall shape of the character and only two pixels difference in the character images, 16 out of 19 meaningful histogram entities are different.

We note that the histograms only serve normalization purposes. In the following, the histograms themselves will **not** be compared. Instead, the comparison will take place on an individual feature (patch) level, across different characters.

Same-Writer Statistics Derivation

The experiments are performed in the following fashion: for given inscriptions' images *I* and *J* with $I \neq J$:

- 1. An empty PVALS array is initialized.
- 2. For each letter l = 1, ..., L, with sufficient character instances present $(M_l > 0, N_l > 0, M_l + N_l \ge 4$; we verify there is enough statistics for a meaningful comparison, slightly lowering the requirements in Ref. 14):
 - 2.1 For each patch p = 1, ..., 512, with at least one nonzero term present in the histogram (i.e., $\exists i_l \cdot H_{i_l}^l(p) > 0$ OR $\exists j_l \cdot G_{j_l}^l(p) > 0$), perform a Kolmogorov–Smirnov (KS) nonparametric

Ψ	Characters' images, patches' counts and frequencies										
Patches											
	1	0.083	1	0.083							
	1	0.083	0	0							
	0	0	1	0.083							
	1	0.083	0	0							
	2	0.167	2	0.167							
	0	0	1	0.083							
	1	0.083	0	0							
	1	0.083	0	0							
	1	0.083	0	0							
	0	0	1	0.083							
	0	0	1	0.083							
	0	0	1	0.083							
	1	0.083	0	0							
	1	0.083	0	0							
	1	0.083	0	0							
	0	0	1	0.083							
	0	0	1	0.083							
	1	0.083	1	0.083							
	0	0	1	0.083							

 Table I. Example of character histograms.

^a Only the meaninful histogrm entries are provided. In both cases, the remaining entries contain zeros. In red – discrepancies between the two histograms.

test between the two samples $\{H_{i_l}^l(p)\}_{i_l=1}^{N_l}$ and $\{G_{j_l}^l(p)\}_{j_l=1}^{N_l}: pval_p^l = KS(\{H_{i_l}^l(p)\}_{i_l=1}^{M_l}, \{G_{j_l}^l(p)\}_{j_l=1}^{N_l}).$ 2.2 Append the resulting $pval_p^l$ to the *PVALS* array.

3. If the *PVALS* array is empty (i.e., no experiments were performed due to the scarcity of data), OR if *I* = *J*, set:

SameWriterP(I, J) = SameWriterP(J, I) = 1.

4. Otherwise utilize the Fisher combination of all the *PVALS* instances, and set:

$$SameWriterP(I, J) = SameWriterP(J, I)$$

= FisherMethod(PVALS)

SameWriterP(I, J) represents the deduced probability of having the same writer in both I and J (the H_0 hypothesis).

A toy-problem illustration of the whole scheme is shown in Figure 2. In this demonstration, two alep letters and four bet letters are segmented from the first document, while three alep and two bet letters are segmented from the second document. As a first step, patches histograms are extracted from the two documents. For illustration

Inscription I:	р	alep1	alep2	bet 1	bet2	bet			
patches' histograms	1	0.02	0.01	0.04	0.03	0.04	4 0.05		
	2	0.18	0.21	0.10	0.09	0.13	L 0.15		
	512	0	0	0	0	0	0		
Inscription II:	р	alep	1 ale	p2 ale	ep 3	bet 3	bet4		
patches' histogram	s 1	0.03	8 0.0	05 0.	06	0.10	0.09		
P	2	0.07	7 0.0	05 0.	19	0.14	0.20		
	512	0	C		0	0	0		
Valid comparisons	Inscripti	on I samp	le Inscri	ption II sam	ple	KS test	: p-value		
Letter=alep, p=1	0.02	, 0.01	0.0	3, 0.05, 0.0	5	0.063			
Letter=alep, p=2	0.18	, 0.21	0.0	7, 0.05, 0.19	Ð	0.425			
Letter=bet, p=1	0.04, 0.03	0.04, 0.05		0.10, 0.09		0.	047		
Letter=bet, p=2	0.10, 0.09	0.11, 0.15		0.14, 0.20		0.	242		
			_						

SameWriter(Inscription1, Inscription2) = FisherMethod(0.063, 0.425, 0.047, 0.242) = 0.0397

Figure 2. An example of the same-writer statistics derivation for two hypothetical inscriptions. Inscription I consists of two instances of the letter *alep*, and four instances of the letter *bet*, while Inscription II consists of three instances of the letter *alep*, and two instances of the letter *bet*. The only patches with enough statistics are patches numbers 1 and 2. Four comparisons of appropriate samples (for each letter and each patch) are performed via Kolmogorov–Smirnov test, resulting in four different *p*-values. These *p*-values are then combined via Fisher's method.

purposes, it is assumed that in both cases, only the first two patches yield a nonzero count. Since two types of relevant features and two different letters are involved, $2 \times 2 = 4$ Kolmogorov–Smirnov tests are performed, yielding four *p*-values. These are combined into a single *p*-value via Fisher's method.

MODERN HEBREW EXPERIMENT The Basic Settings

This experiment closely follows the setting described in Ref. 14. The data set (available at Ref. 30) contains a sampling of 18 individuals, k = 1, ..., 18. Each individual person filled in a Modern Hebrew alphabet table consisting of ten occurrences of each letter, out of the 22 letters in the alphabet (the number of letters and their names are the same as in the Ancient Hebrew in the next experiment; see Figure 3 for a table example). These tables were scanned and thresholded in order to create black and white images. Then their characters were segmented utilizing their known bounding box location (Fig. 3).

From this raw data, a series of "simulated" inscriptions were created. Due to the need to test both same-writer and different-writer scenarios, the data for each writer was split. Furthermore, in order to imitate a common situation in the Ancient Hebrew experiment, where the scarcity of data is prevalent (see below), each simulated inscription used only three letters (i.e., 15 characters; 5 characters for each letter), presenting a welcomed challenge for the new algorithm.

In total, 252 inscriptions were "simulated" in the following manner:

• All the letters of the alphabet except for *yod* (due to its small size), were split randomly into seven groups (three letters in each group), g = 1, ..., 7: *gimel, het,*

10	9	8	7	6	5	4	3	2	1	Letter
k	k	k	/c	k	/c	k	lc	10	k	x alep
ລ	ς	ລ	ລ	Ω	ລ	م	ລ	n	ລ	د bet
2	ç	Ś	٢	٢	ć	ک	5	5	ح	د gimel
3	2	٦	3	3	3	٦	3	3	ه	ד dalet
?	с С	ŝ	ົ	ົ	ŝ	ç	S	0	ۍ	ہ he
/	1)	1)	1	1	/	/)	waw
5	S	٢	5	٢	S	٢	٢	٢	ک	r zayin
n	4	h	n	h	h	n	n	n	r	n het
С	С	С	C	С	С	6	С	6	С	v tet
1	,	'	1	,	,	,	I	1	1	, yod
>	>	2	С	2	>	С	>	د	C	ر kap
б	S	8	S	8	8	б	8	б	б	ל lamed
N	N	N	N	N	N	\sim	Ν	N	N	م mem
ノ	/	/	ノ	/	1	ノ	J	ノ	ノ	ر nun
0	0	0	0	0	0	0	0	0	0	o samek
б	б	б	б	в	Ъ	8	8	б	б	ر ayin
0	0	2	2	ົ	9	9	ົ	9	0	ອ pe
3	3	3	3	3	3	3	3	3	3	¥ sade
P	2	2	P	P	2	Р	P	P	P	qop
2	2	2	С	2	2	2	2	2	2	۲ resh
e	l	e	e	e	e	L	e	e	е	ہ shin
~	ト	ト	5	ア	\searrow	ア	~	ア	ァ	ת taw

Figure 3. An example of a Modern Hebrew alphabet table, produced by a single writer; taken from Ref. 14.

resh; bet, samek, shin; dalet, zayin, ayin; tet, lamed, mem; nun, sade, taw; he, pe, qop; alep, waw, kap.

• For each writer k, and each letter belonging to group g, five characters were assigned into simulated inscription $S_{i,g,1}$, with the rest assigned to $S_{i,g,2}$.

In this fashion, for constant *k* and *g*, we can test if our algorithm arrives at wrong rejection for $S_{i,g,1}$ and $S_{i,g,2}$ (FP = "False Positive" error; 18 writers and seven groups producing 126 tests in total). In addition, for constant *g*, writer *q* s.t. $q \neq k$, and $b, c \in \{1, 2\}$, we can test if our algorithm fails to correctly reject the "same-writer" hypothesis for $S_{k,g,b}$ and $S_{q,g,c}$ (FN = "False Negative" error; 4284 tests in total).

Parameter Tuning and Robustness Verification

The algorithm described in the Algorithm's Description section provides an estimated probability for the H_0 hypothesis ("the two given inscriptions were written by the same writer"). However, two important parameters remain undecided. The first important parameter is the typical area of each character in pixels, leading to the optimal (or at least acceptable) performance. The second crucial parameter is

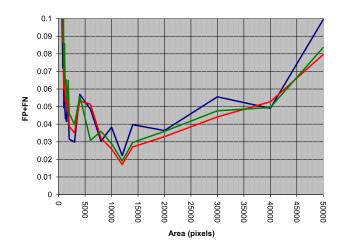


Figure 4. Testing the combined probability of FP + FN errors as a function of character area (in pixels) as well as different *p* value thresholds: 0.2 in blue, 0.1 in red and 0.05 in green. Taking into account the performance in Ref. 14 (FP + FN \approx 0.043), all the tested thresholds and all the areas between 1000 and 40,000 pixels would yield reasonable and comparable performance. Slightly better results are achieved in the range of 8000–20,000 pixels, with 0.1 threshold.

the *p*-value threshold *T*, set for the purpose of rejecting the H_0 .

As is common in statistics, lowering T can result in fewer FP errors, unfortunately increasing the likelihood for FN errors. Conversely, raising T might result in the opposite outcome. In order to minimize the FP and FN errors, a set of simulations was performed. The simulations measured the behavior of the sum FP + FN, with respect to the area of the character's image (ranging from 200 to 50,000 pixels), and to the chosen value of T (attempting the value 0.2 chosen by Ref. 14, as well as the values 0.1 and 0.05, as explained above).

The results of these simulations is shown in Figure 4. Taking into account the performance in Ref. 14 (FP + FN \approx 0.043), all the tested thresholds and all the areas between 1000 and 40,000 pixels yield a reasonable and comparable performance (FP + FN < 0.05), with slightly better results in the range of 8000–20,000 pixels, with T = 0.1. This wide range for acceptable areas indicates an excellent robustness of the algorithm (though the algorithm would probably result in better outcomes if the character images were of similar resolution). Since the mean area of the original character images was 17,367 pixels, well within the reasonable limits of our analysis, we have chosen the typical area of each character to be 17,000 pixels.

Experimental Results

The results of our configuration (for different values of T) are provided in Table II. The results are certainly better than the results of Ref. 14 on the same data set, with a much simpler configuration. As expected, FP error rate tends to zero as the threshold is lowered, while the FN increases slightly. The threshold value of T = 0.1 produced better results, with a combined FP + FN error of less than 2%.



Figure 5. Examples of ostraca (ink inscriptions on clay) from the Iron Age fortress of Arad, located in arid southern Judah. These documents are dated to the latest phase of the First Temple Period in Judah, ca. 600 BCE. The texts represent correspondence of local military personnel.

Table II. Results of modern Hebrew experiment.

Carlinuation		Results		
Configuration	FP	FN	FP + FN	
Results of [14], $T = 0.2$	2.38%	1. 9 4%	4.32%	
Our setting, $T = 0.2$	0.79%	1.70%	2.50%	
Our setting, $T = 0.1$	0.00	1.96%	1.96%	
Our setting, $T = 0.05$	0.00	2.12%	2.12%	

Confident in our newly obtained configuration (target area of \sim 17,000 pixels and T = 0.1), we proceed to the Ancient Hebrew experiment.

ANCIENT HEBREW EXPERIMENT

The Basic Settings

The Ancient Hebrew data set³¹ stems from the Judahite desert fortress of Arad, dated to the end of the First Temple period (Iron Age), ca. 600 BCE—the eve of Nebuchadnezzar's destruction of Jerusalem. The fortress was unearthed half a century ago, with 100 ostraca (ink on clay) inscriptions found during the excavations.³² The inscriptions represent the correspondence of the local military personnel. See Figure 5 for examples of Arad ostraca.

We concentrate on 16 (relatively lengthy) Arad ostraca, two of them two-sided, which brings the total number of texts for analysis to 18. The scarcity of data in this situation is common for these ancient texts. Ostraca images were utilized

Table III. Letter statistics for Arad texts (adapted from Ref. 14).

	Letters													
Text	Alep	He	Waw	Yod	Lamed	Shin	Taw							
1	4	5	3	7	3	3	8							
2	6	3	3	5	3	1	7							
3	2	4	5	4	4	3	3							
5	5	3	1	3	4	2	4							
7	1	2	1	4	6	8	5							
8	2	1	2	1	4	4	2							
16	6	3	9	5	10	3	2							
17a	2	4	2	2	2	1	2							
1 <i>7</i> b		1		2	1	1	2							
18	2	4	4	5	6	6	3							
21	5	4	6	6	12	5	2							
24	9	10	5	8	4	4	7							
31	3	7	6	4	1	1								
38	1	1	2	2	2	1								
39a	3	3	3	5	2	1	1							
39b	3	1	1	4	1									
40	4	5	3	4		3	2							
111	4	3	3	3	1	3	2							

in order to segment and restore the characters stroke by stroke via a variational procedure (detailed in Ref. 20). Some examples in Ref. 14 required minimal human involvement. No further manipulation of the resulting characters' images (e.g., skeletonization, slant correction, etc.) was performed. Table III provides statistics of the most prominent letters, after reconstructing the most legible characters. It can be seen, that even by the modest quantitative standards set in the Algorithm's Description section, for some of the texts the comparisons are barely feasible.

Contrary to the situation in the modern context, now we do not possess any ground truth, indicating the identity of the writers across different inscriptions. Moreover, the experiment's requirements do not impose a strict partition of the texts by their authors. The task is limited to detecting the minimal number of hands within this group of texts. A previous study¹⁴ demonstrated at least four different (pair-wise distinct) writers within the corpus (in fact six different "quadruplets" of texts), while bringing this number to six via textual considerations (not considered in the current article).

As already mentioned, following plausible results of the Modern Hebrew experiment, the characters were resized to 17,000 pixels, and the threshold was set to T = 0.1.

Experimental Results

The results of the experiment are presented in Table IV. The results indicate that there are at least five different (pair-wise distinct) writers within this group of texts. In fact, a closer look at Table IV reveals that three such

	1		1				•	•	• •			IWCCIIICA	-		•			
Text *	1	2	3	5	7	8	16	17a	17b	18	21	24	31	38	39a	39b	40	111
1	1	0.00 0104 451	0.79 4037 056	0.99 7286 098	0.83 5555 244	0.99 9986 905	0.14 5123 589	0.99 9994 862	0.34 5685 406	0.01 2774 181	0.01 2535 286	3.65 925x 10 ⁻¹²	0.01 6073 174	0.07 8182 536	0.03 8794 364	0.30 8694 925	2.97 103x 10 ⁻⁰⁶	0.00 0119 896
2	0.00 0104 451	1	0.99 9999 997	0.23 0810 507	0.23 1039 25	0.99 9837 107	0.78 2882 802	0.99 9377 805	0.12 1018 637	1.96 989x 10 ⁻⁰⁸	0.67 7687 539	0.90 7018 003	0.46 0683 411	1.45 921x 10 ⁻⁰⁷	0.99 9999 999	0.00 4777 329	0.01 1757 086	0.91 8537 018
3	0.79 4037 056	0.99 9999 997	1	0.99 9999 99	1	0.99 9999 995	1	1	0.99 9917 956	4.13 858x 10 ⁻⁰⁷	1	1	0.51 8824 44	0.96 0818 768	1	0.99 9999 219	0.98 3116 915	1
5	0.99 7286 098	0.23 0810 507	0.99 9999 99	1	0.99 9999 996	0.99 9999 979	0.82 9655 242	0.95 5254 622	0.09 3782 225	2.78 436x 10 ⁻¹⁷	0.99 6839 946	4.38 907x 10 ⁻¹⁰	0.02 6192 004	0.02 6797 057	0.94 2902 756	0.86 7249 786	0.04 0887 838	2.13 39x 10 ⁻⁰⁵
7	0.83 5555 244	0.23 1039 25	1	0.99 9999 996	1	0.99 9049 432	0.97 4036 343	0.93 8473 936	0.54 3854 905	6.11 51x 10 ⁻²⁵	0.95 3218 488	0.01 4488 62	0.15 1461 91	0.65 1369 422	0.97 3278 889	0.38 1286 518	0.99 9602 961	0.07 2003 619
8	0.99 9986 905	0.99 9837 107	0.99 9999 995	0.99 9999 979	0.99 9049 432	1	0.99 6867 196	0.99 9999 995	0.26 4813 98	0.00 0160 748	0.99 9994 87	0.99 5623 889	0.49 0501 387	0.02 8988 689	0.99 9933 169	0.61 0834 495	0.99 9979 451	0.81 8431 322
16	0.14 5123 589	0.78 2882 802	1	0.82 9655 242	0.97 4036 343	0.99 6867 196	1	0.91 4322 562	0.98 9523 149	6.53 819x 10 ⁻³⁷	0.99 9999 11	0.05 0144 018	1.82 513x 10 ⁻⁰⁸	0.01 7541 713	0.99 9999 999	0.75 2972 486	0.98 6154 478	0.99 9998 263
17a	0.99 9994 862	0.99 9377 805	1	0.95 5254 622	0.93 8473 936	0.99 9999 995	0.91 4322 562	1	0.98 8381 79	0.99 9824 883	0.98 9761 454	0.91 6602 116	0.99 9934 002	0.97 1750 814	0.99 9957 681	0.99 9885 898	0.75 0470 353	0.99 9999 995
17b	0.34 5685 406	0.12 1018 637	0.99 9917 956	0.09 3782 225	0.54 3854 905	0.26 4813 98	0.98 9523 149	0.98 8381 79	1	0.98 9432 496	0.98 7354 188	0.39 7038 359	0.99 7936 364	0.99 4674 672	0.69 0349 079	0.98 9449 919	0.46 9371 025	0.97 6381 275
18	0.01 2774 181	1.96 989x 10 ⁻⁰⁸	4.13 858x 10 ⁻⁰⁷	2.78 436x 10 ⁻¹⁷	6.11 51x 10 ⁻²⁵	0.00 0160 748	6.53 819x 10 ⁻³⁷	0.99 9824 883	0.98 9432 496	1	1.74 207x 10 ⁻³⁷	2.85 314x 10 ⁻²³	0.87 2302 919	6.42 961x 10 ⁻⁰⁵	0.00 0351 619	3.97 27x 10 ⁻⁰⁵	4.06 656x 10 ⁻¹⁴	0.01 6251 091
21	0.01 2535 286	0.67 7687 539	1	0.99 6839 946	0.95 3218 488	0.99 9994 87	0.99 9999 11	0.98 9761 454	0.98 7354 188	1.74 207x 10 ⁻³⁷	1	0.00 4905 952	0.00 2746 089	0.12 2737 346	0.99 9999 846	0.98 2566 541	0.95 7807 456	0.99 9809 072
24	3.65 925x 10 ⁻¹²	0.90 7018 003	1	4.38 907x 10 ⁻¹⁰	0.01 4488 62	0.99 5623 889	0.05 0144 018	0.91 6602 116	0.39 7038 359	2.85 314x 10 ⁻²³	0.00 4905 952	1	2.93 422x 10 ⁻⁰⁹	0.00 9250 254	0.99 9999 991	0.40 5106 241	6.41 06x 10 ⁻¹²	0.68 4834 031
31	0.01 6073 174	0.46 0683 411	0.51 8824 44	0.02 6192 004	0.15 1461 91	0.49 0501 387	1.82 513x 10 ⁻⁰⁸	0.99 9934 002	0.99 7936 364	0.87 2302 919	0.00 2746 089	2.93 422x 10 ⁻⁰⁹	1	0.85 6161 514	0.99 9999 99	0.99 9884 872	1.70 082x 10 ⁻⁰⁹	0.77 2576 882
38	0.07 8182 536	1.45 921x 10 ⁻⁰⁷	0.96 0818 768	0.02 6797 057	0.65 1369 422	0.02 8988 689	0.01 7541 713	0.97 1750 814	0.99 4674 672	6.42 961x 10 ⁻⁰⁵	0.12 2737 346	0.00 9250 254	0.85 6161 514	1	0.60 0342 228	0.11 2003 203	0.06 7411 667	0.09 1994 45
39a	0.03 8794 364	0.99 9999 999	1	0.94 2902 756	0.97 3278 889	0.99 9933 169	0.99 9999 999	0.99 9957 681	0.69 0349 079	0.00 0351 619	0.99 9999 846	0.99 9999 991	0.99 9999 99	0.60 0342 228	1	0.99 9985 794	0.04 6450 883	1
39b	0.30 8694 925	0.00 4777 329	0.99 9999 219	0.86 7249 786	0.38 1286 518	0.61 0834 495	0.75 2972 486	0.99 9885 898	0.98 9449 919	3.97 27x 10 ⁻⁰⁵	0.98 2566 541	0.40 5106 241	0.99 9884 872	0.11 2003 203	0.99 9985 794	1	0.83 9063 568	0.90 7562 89
40	2.97 103x 10 ⁻⁰⁶	0.01 1757 086	0.98 3116 915	0.04 0887 838	0.99 9602 961	0.99 9979 451	0.98 6154 478	0.75 0470 353	0.46 9371 025	4.06 656x 10 ⁻¹⁴	0.95 7807 456	6.41 06x 10 ⁻¹²	1.70 082x 10 ⁻⁰⁹	0.06 7411 667	0.04 6450 883	0.83 9063 568	1	0.11 3447 052
111	0.00 0119 896	0.91 8537 018	1	2.13 39x 10 ⁻⁰⁵	0.07 2003 619	0.81 8431 322	0.99 9998 263	0.99 9999 995	0.97 6381 275	0.01 6251 091	0.99 9809 072	0.68 4834 031	0.77 2576 882	0.09 1994 45	1	0.90 7562 89	0.11 3447 052	1

Table IV. Results of ancient Hebrew experiment, indicating separation of writers between texts (in darker background).

groups of five pair-wise distinct inscriptions exist, including the following texts: {1, 2, 18, 38, 40}, {1, 18, 24, 38, 40} and {5, 18, 24, 38, 40}. This can be contrasted with Ref. 14, where no such large pair-wise distinct groups were found, despite a higher threshold (T = 0.2). A simple simulation shows that given a random undirected graph of size 16 with an edge probability of 0.1, the probability for having at least three different cliques with at least five members is about 8×10^{-7} ; hence the high statistical significance of the results.

CONCLUSIONS AND FUTURE DIRECTIONS

The current research demonstrates a relatively simple and easily implementable algorithm for the purpose of writer

identification. The algorithm demonstrates highly significant results in a setting including a minimal amount of letters. It is fast and robust with respect to both the typical area of the character images, and the evaluated *p*-value thresholds.

Our approach goes against the common wisdom of combining the different features or metrics before the documents' comparisons takes place. Instead, we propose to perform as many individual experiments as possible on both the letter and feature levels, combining their results only in the end. Although individual building blocks of our algorithm have occasionally been utilized in the literature, our specific amalgamation of binary pixel patterns, Kolmogorov–Smirnov test, and Fisher's method has not been described previously in the literature with regard to writer identification.

Several future development directions and possible enhancements deserve mentioning:

- The size of the patch (3 × 3) can be altered, although even a 4 × 4 patch results in a histogram of length 2¹⁶ = 65,536, which may be too sparse.
- More research regarding target character areas is required. In particular, a more fine-grained approach can be suggested, e.g., areas optimized individually for each letter; areas dependent on characteristic stroke width, etc.
- The algorithm can probably benefit from more aggressive filtering of the incoming input at step 2 (demanding more than four characters in comparison; more than one nonzero histogram item).
- Naturally, our algorithm can benefit from additional tests on other real-world scenarios and data sets, including other languages, writing systems and time periods. This should also include more noisy environments.

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